Infrared Radiation in the Mesosphere and Lower Thermosphere: Energetic Effects and Remote Sensing

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Abstract This paper discusses the formation mechanisms of infrared radiation in the mesosphere and lower thermosphere (MLT), the energetic effects of the radiative absorption/emission processes, and the retrieval of atmospheric parameters from infrared radiation measurements. In the MLT and above, the vibrational levels of the molecules involved in radiative transitions are not in local thermodynamic equilibrium (LTE) with the surrounding medium, and this then requires specific theoretical treatment. The non-LTE models for CO$_2$, O$_3$, and H$_2$O molecules are presented, and the radiative cooling/heating rates estimated for five typical atmospheric scenarios, from polar winter to polar summer, are shown. An optimization strategy for calculating the cooling/heating rates in general circulation models is proposed, and its accuracy is estimated for CO$_2$. The sensitivity of the atmospheric quantities retrieved from infrared observations made from satellites to the non-LTE model parameters is shown.

Keywords Infrared energy · Radiative transfer · Mesosphere lower thermosphere

1 Introduction

In this paper, we concentrate on (a) the role of the infrared (IR) radiation in the energy budget of the mesosphere and lower thermosphere (MLT) as well as (b) on the IR radiation emerging from the atmosphere, which is observed with various instruments from space. Both topics are strongly linked and require detailed consideration of formation and
propagation of the IR radiation in the MLT and its interactions with the various components of the atmosphere.

The translational degrees of freedom of all atmospheric molecular and atomic gaseous compounds represent the heat reservoir. This reservoir obtains or loses energy due to a number of sources and sinks, among them heating and cooling related to various types of mass motions, redistribution of energy released in the course of various photochemical reactions (the translational energy, the chemical energy and the nascent electronic, vibration and rotational energy of the reaction products), and absorption and emission of the IR radiation. In the latter case, one usually speaks about the interaction between matter and the IR radiative field, which, for the case of the MLT, includes the atmospheric radiation formed in these layers, the upwelling radiation from the ground and lower atmosphere, and, during daytime, the IR solar radiation.

Our primary interest here is with the interaction of the heat reservoir and the IR radiative field. The energy exchange between them is carried out through an intermediate reservoir of vibrational and rotational energy of molecular atmospheric compounds: the photons are absorbed and emitted by molecules of optically active gases through the processes of spontaneous and stimulated emission and absorption in a large variety of molecular rotational-vibration and rotational transitions. In this respect, the MLT has a significant peculiarity related to the fact that the translational (and in its upper part also rotational) excitation of the molecules does not obey Boltzmann’s law with the local kinetic temperature. As a result, the IR radiation (which is often called “thermal radiation”) emitted in these layers does not reflect the thermal state of matter. This situation is referred to as the breakdown of local thermodynamic equilibrium (LTE) for the vibrational or rotational–vibrational degrees of freedom. Detailed treatment of non-LTE plays a crucial role for the estimation of the thermal effects of the IR radiation and for the diagnostics of space-based IR observations.

In the book by López-Puertas and Taylor (2001), the discussion of both topics was presented relying on the current status of research at that time. Since then, many research papers have been published in this field. For example, the recent paper of Funke et al. (2012) contains an updated compilation of the non-LTE models for the most important atmospheric infrared emitters. However, no reviews discussing the current status of methodologies and indicating the directions for further studies have been published for quite a while. This paper is intended (at least partly) to fill this gap. The storyline is built around the studies in which both authors took part and, naturally, other works that to our mind had a significant impact on the field.

The paper is organized as follows. First, we consider the mechanisms of the IR radiation generation in the MLT, discuss the conditions for LTE breakdown using an example of a two-level atom (Sect. 2), and introduce the radiative cooling/heating rate (called “heating rate” throughout this paper, see the definition in Sect. 2.2.4), which is the characteristic essential for understanding the energetic balance in the MLT. This section also contains a description of the research code that is used for all test calculations shown in this work.

Section 3 provides the current status of our non-LTE model for carbon dioxide, ozone, and water vapor, the three most important molecules for the IR heating of the MLT. For each of the molecules considered, the calculated heating rates for five typical atmospheric scenarios, from subarctic summer to subarctic winter, are shown. We pay specific attention to the problem of the quenching rate coefficient for energy exchange during CO$_2$–O collisions and provide details of the most recent study on this topic. We discuss the O$_2$/O$_3$ photolysis scheme and the coupling of the photolysis products’ energy levels with the system of water vapor vibrational levels. At the end of Sect. 3, we consider an interesting aspect of the
radiative cooling in the MLT that is related to the combined effect of the small-scale temperature and trace gas concentration fluctuations associated with gravity waves, and to the radiative transfer in the 15 \( \mu m \) CO\(_2\) band. Section 4 deals with the optimization of the heating rate calculations necessary for atmospheric modeling. Besides the well-known parameterization methods, we also present an approach that provides accuracy comparable to line-by-line calculations but is faster by a factor of \( \sim 10^3 \)–\( 10^4 \). Section 5 describes the most common techniques of IR sounding of the MLT and peculiarities of the atmospheric parameter retrievals related to the non-LTE character of radiation emitted from this region. Section 6 presents the conclusions of this work.

2 IR Radiation in the MLT: Generation Mechanisms and Interaction with Matter

2.1 Overview

Optically active molecular gases at any given height in the atmosphere absorb and emit radiation. With respect to the radiative energy transformations, the MLT area can be considered as a mixture of gases exposed to (a) the solar irradiance from the top, (b) the reflected solar radiation from below, (c) the terrestrial IR radiation from below, and (d) the radiation emitted by the molecules in other atmospheric layers (Fig. 1). Solar energy is absorbed primarily by O\(_2\) and O\(_3\) molecules, and their photolysis leads to atmospheric heating both directly (through the formation of translationally hot products) and by creating electronically and vibrationally excited products that later will heat the atmosphere through a set of energy exchange processes. The solar near-infrared radiation in the spectral range with wavelengths \( \lambda \leq 5 \mu m \) is also absorbed by a number of molecules to provide the heating of the MLT; among them, the most noteworthy are the CO\(_2\) 2.0, 2.7, and 4.3 \( \mu m \) bands. Another source of the MLT heating is the absorption of atmospheric radiation emitted from other atmospheric layers. This heating is accompanied by cooling due to the emission of radiation, mainly in the CO\(_2\) 15 \( \mu m \) band, O\(_3\) 9.6 \( \mu m \) band, and H\(_2\)O rotational and 6.3 \( \mu m \) vibrational bands (e.g., see Brasseur and Solomon 2005). In this work, we will focus mainly on the IR part of the spectra that corresponds to the rotational–vibrational (also called ro-vibrational) transitions of the atmospheric molecules.

If a molecule (or atom) is formed in an excited state due to absorption of a radiation quantum or due to chemical or photochemical processes, then the energy of excitation may be (a) emitted to the atmosphere; (b) transferred to another excited state of the same molecule through an intra-molecular energy exchange induced by collision with another molecule or atom; (c) transferred to other molecules by intermolecular vibrational–vibrational (V–V) or (d) electronic-vibrational (E–V) energy exchange processes; or (e) converted to kinetic energy of atmospheric molecules and atoms via collision (vibrational–translational energy exchange, V–T). A simplified scheme of the interactions between the atmospheric molecules is shown in Fig. 2. In general, each molecule exchanges energy with the heat reservoir through the V–T collisions and interacts with other molecules through a set of V–V and E–V energy exchanges.

To calculate the absorbing and emitting characteristics of the optically active molecules and to estimate the balance between the IR cooling and heating one needs to know the populations of the corresponding ro-vibrational levels. However, as mentioned above, the vibrational levels of the molecules under consideration are not in thermodynamic equilibrium with the surrounding medium in the MLT. The next section provides the background necessary for understanding the non-LTE effects in the atmosphere.
2.2 LTE and Non-LTE

2.2.1 The Two-Level Atom

For simplicity, let us first consider a case of a plane-parallel atmosphere that contains just one optically active component: a two-level hypothetical atom. Let us assume that we...
consider a steady state of the atomic gas, which means that pressure, temperature, and the degree of excitation (the ratio of the upper-level population to the lower-level population) do not change with time. For this atom, one can write the steady-state equation (SSE), which describes the various processes populating and de-populating each level of the atom at any given altitude, as

\[(R_{21} + C_{21}) \cdot n_2 = (R_{12} + C_{12}) \cdot n_1,\]  \(1\)

where \(n_1\) and \(n_2\) are the populations of the first and second levels, respectively, \(C_{12}\) and \(C_{21}\) are the coefficients of collisional population and de-population of the second level, and

\[R_{21} = A_{21} + B_{21} \cdot \bar{J}(z), \quad R_{12} = B_{12} \cdot \bar{J}(z)\]  \(2\)

are the radiative terms, where \(A_{21}\), \(B_{21}\), and \(B_{12}\) are, respectively, the Einstein coefficients for spontaneous emission, stimulated emission, and absorption, and

\[\bar{J}(z) = \frac{1}{4\pi} \int d\Omega \int_\infty^{-\infty} I_{\mu\nu}(z) \varphi(\nu, z) d\nu = \int_1^{-1} \int_\infty^{-\infty} I_{\mu\nu}(z) \varphi(\nu, z) d\nu d\mu\]  \(3\)

is the integrated mean intensity of the radiation at the considered altitude. Here, \(I_{\mu\nu}(z)\) is the monochromatic radiation intensity, which satisfies the radiative transfer equation (RTE)

\[\mu \frac{dI_{\mu\nu}(z)}{dz} = -\chi_{\mu\nu}(z)I_{\mu\nu}(z) + \eta_{\mu\nu}(z),\]  \(4\)

where \(I_{\mu\nu}(z)\) is the monochromatic radiation intensity, \(\mu = \cos(\theta)\) is the direction cosine, \(\nu\) is the frequency of the radiation, \(\chi_{\mu\nu}(z)\) and \(\eta_{\mu\nu}(z)\) are the total opacity and emissivity, respectively, and \(\varphi(\nu, z)\) is the normalized spectral line profile function, which satisfies

\[\int_\infty^{-\infty} \varphi(\nu, z) d\nu = 1.\]  \(5\)

It is important to note that the opacity and emissivity terms in \(4\) are expressed through the populations of the upper and lower levels as \(\chi(z) = \frac{\hbar}{4\pi} (n_1(z)B_{12} - n_2(z)B_{21})\) and \(\eta(z) = \frac{\hbar}{4\pi} n_2(z)A_{21}\), respectively. In order to find \(n_1\) and \(n_2\), one must supplement Eq. \(1\) by the particle conservation law

\[n_1 + n_2 = 1.\]  \(6\)

In general, \(\bar{J}(z)\) in the radiative terms \(R_{21}\) and \(R_{12}\) in \(2\) in the MLT is the combination of solar radiation, terrestrial radiation, radiation scattered by the clouds, and the atmospheric radiation (see Fig. 1). The system of steady-state Eqs. \(1\) and \(6\) can be solved for the populations \(n_1\) and \(n_2\) if all the coefficients \(A_{21}, B_{21}, B_{12}, C_{21}, C_{12},\) and \(\bar{J}(z)\) are known. On the other hand, finding \(\bar{J}(z)\) requires solving and integrating the radiative transfer Eq. \(4\), which depends on the populations \(n_1\) and \(n_2\). As a result, one has to search for the joint solution of \(1\), \(6\) and \(3\), \(4\) (e.g., see Ivanov 1973; Mihalas 1978). There are various approaches to solving this joint system in atmospheric studies: the Curtis method (e.g., see Goody and Yung 1995), Lambda Iterations (e.g., see Wintersteiner et al. 1992), Modified Curtis Method (e.g., see López-Puertas and Taylor 2001; Funke et al. 2012), Accelerated Lambda Iterations (e.g., see Kutepov et al. 1998; Gusev and Kutepov 2003). We will refer to them in Sect. 4.1 with respect to the calculation optimization schemes.
In further consideration of the two-level system, one has to keep in mind that the coefficients $C_{12}$ and $C_{21}$ in (1) are linked by the detailed balance equation

$$C_{21} = C_{12} \frac{g_2}{g_1} e^{-E_{21}/kT},$$  \hspace{1cm} (7)

where $k$ is Boltzmann’s constant, $E_{21}$ is the energy difference between the levels, and $T$ is the local temperature. This results from the validity of the Maxwellian distribution for the translational degrees of freedom for molecules and atoms of the atmospheric constituents in the MLT. Correspondingly, if the terms $R_{12}$ and $R_{21}$ in Eq. (1) are negligible in comparison with $C_{12}$ and $C_{21}$ or if $n_1R_{12} \approx n_2R_{21}$, then the populations $n_1$ and $n_2$ will obey Boltzmann’s law. Since the collisional term is proportional to the concentration of the collisional partner, the former situation is typical for the lower atmosphere. The latter situation is possible in the cores of optically thick lines. This is also more typical for the lower atmosphere due to high concentrations of the absorbing gas. We will refer to such conditions as “LTE” (local thermodynamic equilibrium) and we will denote the corresponding level populations as the “LTE populations”. If the frequency of collisions is low and $n_1R_{12} \neq n_2R_{21}$, then the populations will be sensitive to the radiative field. This situation is called “non-LTE”.

2.2.2 The Multi-Level Non-LTE Problem

In reality, the number of levels involved in energy exchange processes in the atmosphere is far greater than two (see Figs. 7, 11, 14 below). In this case, the system of SSE (1), (6) and RTE (4) must be extended to the other levels. Correspondingly, a complete system for $N_V$ vibrational levels will include $N_V$ steady-state equations, one of which must be replaced by a particle conservation equation similar to (6). In the case of a multi-level problem, the collisional terms are divided into two groups: V–T, for which the vibrational state of only one collisional partner changes, and V–V energy exchange processes, for which both of the collisional partners change their vibrational states. In general form, the steady-state equation for a multilevel problem involving chemical production $P$ and losses $L$ can be written as:

$$n_l \left( L_l + \sum_{l' \neq l} (R_{ll'} + C_{ll'}) \right) = \sum_{l' \neq l} n_{l'} (R_{l'l} + C_{l'l}) + P_l \quad (l = 1, 2, \ldots, N_V).$$  \hspace{1cm} (8)

Each of the molecules considered is characterized by a set of radiation coefficients, usually obtained from the HITRAN spectroscopic database described in Rothman et al. (2009), and by a set of V–T and V–V rates representing a compilation of the most up-to-date measurements and theoretical calculations.

For the case of a multilevel problem with rotational substructure of vibrational levels, the integrated mean intensity calculation (3) and the radiative transfer Eq. (4) must take into account the ro-vibrational structure of the optical molecular band. In general, for any given pair of ro-vibrational levels ($l, l'$), where $l'$ is the lower level index and $l$ is the upper level index, the emissivity $\eta_{ll'}(v)$ and opacity $\chi_{ll'}(v)$ at the frequency $v$ are given by

$$\eta_{ll'}(v) = \frac{hv_{ll'}}{4\pi} n_l A_{ll'} \phi_{ll'}(v), \quad \chi_{ll'}(v) = \frac{hv_{ll'}}{4\pi} (n_l B_{ll'} - n_l B_{ll'}) \phi_{ll'}(v),$$  \hspace{1cm} (9)

where $v_{ll'}$ is the line center frequency, $A_{ll'}$, $B_{ll'}$, and $B_{ll'}$ are the Einstein coefficients, and $\phi_{ll'}(v)$ is the normalized line profile (see (5)). The total emissivity and opacity expressed in terms of line quantities (9) are
\[ \eta(v) = \sum_{I,F} \eta_{IF}(v), \quad \chi(v) = \sum_{I,F} \chi_{IF}(v). \] (10)

In the traditional approach, the radiative transfer equation is solved for each line separately, and the resulting integrated mean intensities are summed for the molecular band considered. This type of radiative transfer calculations is called LBL (for line-by-line) and is used as a reference because of its high accuracy. The computational cost is high, due to the large number of individual lines involved. In addition, each line in this approach must be well resolved at all altitudes, which means that a large number of spectral points must be considered. In the lower atmosphere, the problem is complicated by line overlapping, which requires a finer spectral grid. Fortunately, in the Earth’s atmosphere, line overlapping effects are essentially separated from the non-LTE effects: the lower the pressure, the narrower the line and the stronger the non-LTE effects. In this work, we will consider only non-overlapping lines, which is a reasonable approximation for the MLT. We will address the computational cost issues and the optimization strategy in the Sect. 4. For more details regarding solving the multi-level non-LTE problem, we refer the reader to the works of Kutepov et al. (1998), López-Puertas and Taylor (2001), and Gusev and Kutepov (2003).

\[ T_{\text{vib}} = \frac{n_l}{n_0} \frac{E_l}{E_0} e^{-(E_l-E_0)/kT_{\text{vib}}}, \] (11)

where \( E_l \) is the energy of the level \( l \) and \( E_0 \) is the ground-level energy. If the level is in LTE, then \( T_{\text{vib}} = T_{\text{kin}} \). If \( T_{\text{vib}} > T_{\text{kin}} \) then the net pumping of the level is larger than that under LTE conditions. Similarly, if \( T_{\text{vib}} < T_{\text{kin}} \), the level is populated less efficiently and/or depopulated faster than at LTE.

Let us comment on the behavior of the corresponding \( T_{\text{vib}} \) in Fig. 3 and explain the physics involved: the temperature difference between the stratopause and the mesopause is not high enough to ensure significant pumping of the 01101 levels by radiation coming from below (see the right-hand panel of Fig. 3); the high optical thickness of the main isotope’s \( v_2 \) transitions and frequent atmospheric collisions keep the 626(01101) level in LTE up to \( \sim 80 \) km altitude; the 638(01101) level is characterized by optically thinner
“photon escape paths” that leads to LTE breakdown for this level at lower altitudes; the absorption of solar radiation and its further redistribution to the 00011 levels moves them out of LTE at $\sim 55$ km altitude. The level 20012 is efficiently pumped by solar radiance absorption in the 2.0-$\mu$m band and is in non-LTE even at low altitudes. Following this logic, one may explain the $T_{\text{vib}}$ behavior in other cases.

2.2.4 Radiative Cooling and Heating Rates

Radiative cooling and heating are essential energetic characteristics of the atmosphere that show the amount of energy acquired or lost by an atmospheric layer due to the integrated effects of radiative energy absorption and emission. The radiative flux divergence defines the rate at which energy is added to the radiative field per unit volume, that is the rate at which energy is lost by the matter. Following the standard way (see, e.g., Goody et al. 1989), we introduce the radiative heating rate $h$ for this process as the radiative flux divergence taken with the minus sign. In the plane-parallel atmosphere at the altitude $z$, the flux divergence is obtained by integrating Eq. (4) over frequency and solid angle

$$h(z) = -\frac{1}{4\pi} \int_{\Omega} d\Omega \int_{-\infty}^{+\infty} \mu \frac{dI_{\nu\nu}(z)}{dz} dv$$  \hspace{1cm} (12)

Since the main effect of interaction between the infrared radiation and the atmosphere is cooling, $h(z)$ is often called “cooling rate”, even though it is a heating rate by definition. One has to keep in mind that $h(z)$ may be both positive (heating) and negative (cooling) depending on the dominating term in the right-hand side of Eq. (12). Throughout this paper, we will call
the heating rate”. The units of \( h(z) \) in (12) are (W/m\(^3\)). To convert the \( h(z) \) values to units more commonly used in atmospheric physics (K/day), one has to apply the formula

\[
h(z) \text{(K/day)} = h(z) \text{(W/m}^3\text{)} \cdot \frac{24 \cdot 60 \cdot 60}{C_p(z) \rho(z)},
\]

where \( C_p(z) \) is the heat capacity at constant pressure in (J/kg/K), and \( \rho(z) \) is the density in (kg/m\(^3\)). We note here that heating rate in (K/day) should not be treated as daily averages; “day” is used as time unit while \( h(z) \) can (and does) vary during the day. We suppose that the integral over frequency in (12) covers the entire IR range and will show the altitude distributions for the net heating rate \( h(z) \). The sign of \( h(z) \) tells whether the atmosphere is cooled or heated at the given altitude \( z \), and its magnitude provides an estimate of the importance of a given molecule for the energetic balance of the region. The heating rate distributions will be accompanied by plots showing the \( n_l(z) \) distributions for the most important vibrational levels. In Sect. 3, we will consider the non-LTE radiative heating rates for the main contributors to the MLT radiative energy budget: CO\(_2\), O\(_3\), H\(_2\)O, and the kinetics of the O\(_2\)/O\(_3\) photolysis products.

2.3 ALI-ARMS Research Code

All calculations presented in this work were performed with the help of the ALI-ARMS (for Accelerated Lambda Iterations for Atmospheric Radiation and Molecular Spectra) non-LTE code package described in detail in Kutepov et al. (1998), Gusev and Kutepov (2003), and Gusev (2003). Compared to the other non-LTE codes applied in the studies of the Earth’s and planetary atmospheres, the ALI-ARMS code solves the multi-level problem (8) by means of the accelerated lambda iteration (ALI) technique developed in stellar astrophysics (e.g., see Rybicki and Hummer 1991, 1992; Pauldrach et al. 1994, 2001; Pauldrach 2003; Hubeny and Lanz 2003; Hubeny et al. 2003) for calculating non-LTE populations of atomic and ionic levels (see also Sect. 4.1 of this paper).

The code in its current version can treat an arbitrary number of molecules of arbitrary structures in a given planetary atmosphere provided by the prescribed format inputs of (a) planetary atmosphere profile that consists of pressure, temperature, volume mixing ratios (VMRs) of molecules at all altitudes, (b) solar spectra, (c) vibrational and ro-vibrational energies, (d) spectroscopic information (the Einstein coefficients for ro-vibrational or rotational transitions, line half-widths), and (e) collisional rate coefficients for specified sets of E–V, V–T, and V–V transitions. The code produces populations of ro-vibrational levels and radiative flux divergences (radiative cooling and heating) in the lines and bands involved.

The current inputs of V–T and V–V rates are described in Shved et al. (1998), Manuilova et al. (1998) and summarized in the Ph.D. thesis by Gusev (2003). These inputs include the interactions between the following molecules: N\(_2\), O\(_2\), CO\(_2\), O\(_3\), H\(_2\)O, CO, OH, and NO (Fig. 2). The reference model (Fig. 4) includes 350 vibrational levels and 200,000 ro-vibrational lines of the CO\(_2\) molecule and its isotopes (Sect. 3.1), 23 vibrational levels and 150,000 ro-vibrational lines of ozone (Sect. 3.2), 14 vibrational levels and 20,000 lines of the H\(_2\)O molecule (Sect. 3.4), and 7 vibrational levels of N\(_2\) molecule. The model also incorporates the kinetic model of O\(_2\)/O\(_3\) photolysis products (Sect. 3.3) developed by Yankovsky and Manuilova (2006) and interactions of the photolysis products with vibrational levels of H\(_2\)O, N\(_2\), and CO\(_2\) molecules.

The ALI-ARMS code has been successfully applied to the interpretation of the 4.3- and 9.6-\(\mu\)m spectral Earth’s limb radiation measured by the Cryogenic Infrared Spectrometers and Telescopes for the Atmosphere (CRISTA) instrument (see Offermann et al. 1999;
Grossmann et al. (2002) in the studies by Kaufmann et al. (2002, 2003) who retrieved the first global CO$_2$ and O$_3$ density distributions in the Earth’s MLT. Later Gusev et al. (2006) applied the ALI-ARMS model to the analysis of the CRISTA 15 μm spectral radiation data and performed temperature retrievals in the MLT. The ALI-ARMS code was used for the analysis (see Maguire et al. 2002) of the seasonal, altitude, and latitude variations of the 10 μm CO$_2$ limb emissions measured by the Thermal Emission Spectrometer onboard the Martian Global Surveyor (TES/MGS), as well as to study the infrared radiative heating of the middle and upper atmospheres of Mars (see Hartogh et al. 2005) and Earth (e.g., see Kutepov et al. 2007).

The ALI-ARMS code was also used (see Kutepov et al. 2006, Feofilov et al. 2009, Rezac 2011) for the validation of the operational retrieval algorithms applied to processing broadband 15 and 4.7 μm CO$_2$ and 6.3 μm H$_2$O Earth’s limb emissions measured by the SABER (Sounding of the Atmosphere using Broadband Emission Radiometry) instrument (see Russell et al. 1999) on board the NASA TIMED (Thermosphere Ionosphere Mesosphere Energetics and Dynamics) satellite (see Yee et al. 1999). It was also used for the analysis of the MGS-TES 15 μm limb observations to extend temperature retrievals in Martian atmosphere up to ~90 km altitude (see Feofilov et al. 2012b) and for developing the two-channel algorithm for simultaneous retrieval of pressures/temperatures and CO$_2$ VMRs in the MLT from the SABER limb 15 and 4.3 μm radiation (see Rezac 2011).

2.4 Test Atmospheres Used in Study

To demonstrate the variability of the infrared energy budget components in the MLT, we used five typical atmospheric scenarios. The time of the year for all of the test profiles was...
set to the summer solstice in the Northern hemisphere. The time of the day was set to local noon. Pressure/temperature profiles, O\(_2\), and N\(_2\) VMR profiles were obtained from the MSIS-E-90 database (http://omniweb.gsfc.nasa.gov/vitmo/msis_vitmo.html). The CO\(_2\) VMRs were taken from WACCM model outputs (http://waccm.acd.ucar.edu/). Because the O\(_3\), O\(_3\)(P), and O\(_1\)(D) values are highly variable and are interdependent, we used the correspondent VMRs obtained from the SABER V1.07 “instantaneous” retrievals (http://saber.gats-inc.com/). The H\(_2\)O VMRs are July averages retrieved from all ACE-FTS measurements (see Bernath et al. 2005). In this work, we will use abbreviated names for these five atmospheric scenarios: SAW for subarctic winter, MLW for midlatitude winter, TROP for the tropical atmosphere, MLS for midlatitude summer, and SAS for subarctic summer. The latitudes and solar zenith angles for local noon, \(\theta_z\), and the SABER 2010 orbits and record numbers are listed in Table 1.

Figure 5 shows the temperature profiles used in the study. These profiles cover most of the situations that are observed in the atmosphere, unperturbed by gravity waves (GW, see Sect. 3.5).

Even though the area of our primary interest is the MLT, pressure/temperature and trace gases VMR distributions in the lower atmosphere are also necessary due to non-local effects and pumping the molecular levels in the MLT by radiation coming from below. Some features of the selected profiles are worth noting: the stratopause temperature varies from 255 K (MLW) to 281 K (SAS), the mesopause temperature changes from 140 K (SAS) to 200 K (SAW) (see the discussion in Smith 2012), and the \(\theta_z\) changes from 16.5° (MLS) to 93.5° (SAW). One has to keep in mind that even though \(\theta_z = 93.5° > 90.0°\) means night on the ground, the SAW atmosphere is in shadow only up to \(~12\) km while, above this point, the atmosphere is still illuminated so this specific case is called “twilight” in Table 1. The maximum of the solar pumping and O\(_2\)/O\(_3\) photodissociation in this case moves up, contrary to the low \(\theta_z\) case for MLS atmospheric scenario. Figure 6 shows the vertical distributions of the CO\(_2\), O\(_3\), H\(_2\)O, O\(_3\)(P), and O\(_1\)(D) VMRs. It is essential to include both daytime and nighttime ozone profiles because of the second ozone maximum at \(~90\) km during the nighttime.

### Table 1 Atmospheric scenarios used in this study

<table>
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<tr>
<th>Name</th>
<th>Day/night</th>
<th>SAW Day/night</th>
<th>MLW Day/night</th>
<th>TROP Day/night</th>
<th>MLS Day/night</th>
<th>SAS Days</th>
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<td>63.5°</td>
<td>23.5°</td>
<td>16.5°</td>
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<td>194</td>
<td>193</td>
<td>193</td>
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<tr>
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<td>0.1°N</td>
<td>38.0°N</td>
<td>68.4°N</td>
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<tr>
<td>SABER day Longitude</td>
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<td>192</td>
<td>192</td>
<td></td>
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<tr>
<td>SABER night Latitude</td>
<td>68.14°S</td>
<td>40.0°S</td>
<td>0.1°S</td>
<td>38.1°N</td>
<td>–</td>
<td></td>
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<tr>
<td>SABER night Longitude</td>
<td>208.1°</td>
<td>273.5°</td>
<td>318.6°</td>
<td>175.9°</td>
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<td></td>
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<tr>
<td>SABER night (\theta_z)</td>
<td>131.0°</td>
<td>154.8°</td>
<td>154.5°</td>
<td>119.4°</td>
<td></td>
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</table>
3 Radiative Cooling and Heating in the MLT

The main objective of this section is to provide an overview of CO₂, O₃, O₂, and H₂O contributions to the energy budget of the MLT, and to discuss the energy transformation mechanism in which these molecules are involved. This requires considering the non-LTE models for the CO₂, O₃, and H₂O molecules as well as the model of O₂/O₃ photolysis products kinetics.

3.1 Carbon Dioxide

Carbon dioxide is an optically active linear triatomic molecule. It has the three vibrational modes: linear symmetric and asymmetric stretch vibrations referred to as ν₁ and ν₃, respectively, and bending mode (ν₂). The vibrational quanta energies are 1,388, 667, and 2,349 cm⁻¹ for ν₁, ν₂, and ν₃ modes, respectively. The CO₂ vibrational levels diagram with the main optical transitions and processes of V–V exchange is shown in Fig. 7. The levels on this diagram are marked in accordance with the HITRAN notation described in Sect. 2.2.3. A CO₂ molecule takes part in the following processes essential for the MLT energetics: solar radiation absorption in 1–4.3-μm bands, CO₂ atmospheric radiation absorption and emission, and redistribution of the excitation among various vibrational levels in a series of V–V, V–T, and emission processes.

Let us consider in detail the 15-μm infrared emission (I₁₅ μm) formation. This emission is the dominant cooling mechanism in the Earth’s MLT (e.g., see Gordiets 1976; Dickinson 1984; Goody and Yung 1995; Sharma and Wintersteiner 1990). On Earth, the magnitude of the MLT cooling affects both the mesopause temperature and height; the stronger the cooling, the colder and higher is the mesopause (see Bougher et al. 1994). The main
processes linking the 15-μm CO₂ atmospheric radiation to the heat reservoir (translational degrees of freedom of atmospheric constituents) are the inelastic collisions of CO₂ molecules with O\(^{(3P)}\) atoms: first, O\(^{(3P)}\) atom excites the CO₂ bending vibrational mode during the collision:

\[
\text{CO}_2 (m_2) + \text{O}^{(3P)} \rightarrow \text{CO}_2 (m_2 + 1) + \text{O}^{(3P)},
\]

after which the excitation may be (a) quenched by another collision with some molecule or atom, (b) transferred to excited vibrational state of another molecule through the V–V exchange, or (c) transformed to a quantum of radiation: CO\(_2(v_2 + 1) \rightarrow \text{CO}_2(v_2) + h\nu\) (667 cm\(^{-1}\)). To be consistent with the generally accepted way of describing this process, we will refer to the rate coefficient of the reaction inverse to (14) and will call it the “CO₂–O quenching rate coefficient” or \(k_{VT}\), where VT stands for vibrational–translational type of interaction. Generally, it is assumed that the velocity distribution of O\(^{(3P)}\) atom is Maxwellian and that the fine structure of atomic oxygen does not affect the process (14) and its inverse. We will discuss the validity of these assumptions later in Sect. 3.1.2.

Both the radiative heating and \(I_{15\ \mu m}\) strongly depend on \(k_{VT}\), see Sect. 3.1.2. It is, therefore, self-evident that both the calculation of radiative heating rates in CO₂ and the interpretation of measured \(I_{15\ \mu m}\) radiation require the best possible knowledge of \(k_{VT}\). However, despite the importance of \(k_{VT}\) for the atmospheric applications, the values, obtained in a laboratory and retrieved by fitting the space observations, vary by a factor of 3–4 (see Table 2). We draw attention to the uncertainty of the \(k_{VT}\) quenching rate since its effects on the cooling are comparable to the contributions of all the other radiative heating mechanisms as illustrated below.

### 3.1.1 Sensitivity of MLT Cooling to the \(k_{VT}\) Quenching Rate

Fig. 6 Volume mixing ratios of CO₂, O₃, H₂O, O\(^{(3P)}\) and O\(^{(3D)}\) used in heating rate calculations, infrared radiation profile estimates, and testing the optimized heating rate calculation schemes: (a) SAW, (b) MLW, (c) TROP, (d) MLS, (e) SAS

Fig. 6 Volume mixing ratios of CO₂, O₃, H₂O, O\(^{(3P)}\) and O\(^{(3D)}\) used in heating rate calculations, infrared radiation profile estimates, and testing the optimized heating rate calculation schemes: (a) SAW, (b) MLW, (c) TROP, (d) MLS, (e) SAS
of five test atmospheres described in Sect. 2.4, we solved the non-LTE problem twice. In
the first run, $k_{VT}$ was set to $1.5 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$, the value that is close to laboratory
measurements (see Table 2). For the second run, $k_{VT}$ was set to $6.0 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$,
which is typically retrieved from atmospheric measurements. A standard $(T/300)^{1/2}$ scaling
factor for the temperature dependence of the $k_{VT}$ was used. In these calculations, we
applied the CO$_2$ non-LTE model that included 60 vibrational levels of 5 CO$_2$ isotopes as
well as the first excited vibrational levels of N$_2$ and O$_2$. Compared to our extended
reference model of CO$_2$ described in Sect. 2.3, this reduced model is accurate within
0.05 K for the CO$_2$(v$_2 = 1, 2$) vibrational temperatures and 0.03 K/day for net CO$_2$ radi-
ative cooling and heating rates. The results are presented in Figs. 8 and 9. Figure 8 shows
the response of two CO$_2$(v$_2$) levels of the main isotope to $k_{VT}$ changes. As one can see, for
all five of the test atmospheres, the non-LTE effects become noticeable above ~80 km altitude.

The altitudinal behavior of the CO$_2$(v$_2$) level populations has the same pattern for all
five model atmospheres: the populations move farther from LTE with increasing height.
The deviation from LTE depends on the atmospheric scenario: SAW, MLW, and TROP
atmospheres demonstrate weaker non-LTE effects compared to MLS and, especially, SAS
atmospheres. This is explained by larger temperature differences between the stratopause
temperatures and the mesospheric temperatures in the latter two models: the warmer
stratopause region produces stronger upwelling $I_{15 \mu m}$ radiation flux, which pumps CO$_2$(v$_2$)
levels in the MLT. The response of the CO$_2$(v$_2$) levels population to the V–T rate coeffi-
cient is straightforward (compare blue curves in Fig. 8a–d to the red ones): higher $k_{VT}$
leads to more efficient thermalizing of the CO$_2$(v$_2$) levels and moves their vibrational

![CO$_2$ vibrational levels diagram](image-url)
Table 2 Historic review of the $k_{VT}$ quenching rate coefficient laboratory measurements and atmospheric retrievals at $T = 300$ K

<table>
<thead>
<tr>
<th>$k_{VT}$ (cm$^3$ s$^{-1}$)</th>
<th>Reference</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>$3\times 10^{-14}$</td>
<td>Crutzen (1970)</td>
<td>First guess</td>
</tr>
<tr>
<td>$2.4 \times 10^{-14}$</td>
<td>Taylor (1974), Center (1973)</td>
<td>Laboratory measurements</td>
</tr>
<tr>
<td>$5.0 \times 10^{-13}$</td>
<td>Sharma and Nadile (1981)</td>
<td>Atmospheric retrieval</td>
</tr>
<tr>
<td>$1.0 \times 10^{-12}$</td>
<td>Gordiets et al. (1982)</td>
<td>Numerical experiment</td>
</tr>
<tr>
<td>$2.0 \times 10^{-13}$</td>
<td>Kumer and James (1983)</td>
<td>Atmospheric retrieval</td>
</tr>
<tr>
<td>$2.0 \times 10^{-13}$</td>
<td>Dickinson (1984), Allen et al. (1980)</td>
<td>Laboratory measurements</td>
</tr>
<tr>
<td>$5.2 \times 10^{-12}$</td>
<td>Stair et al. (1985)</td>
<td>Atmospheric retrieval</td>
</tr>
<tr>
<td>$3.5 \times 10^{-12}$</td>
<td>Sharma (1987)</td>
<td>Atmospheric retrieval</td>
</tr>
<tr>
<td>$3-9 \times 10^{-12}$</td>
<td>Sharma and Wintersteiner (1990)</td>
<td>Atmospheric retrieval</td>
</tr>
<tr>
<td>$1.5 \times 10^{-12}$</td>
<td>Shved et al. (1991)</td>
<td>Laboratory measurements</td>
</tr>
<tr>
<td>$1.3 \times 10^{-12}$</td>
<td>Pollock et al. (1993)</td>
<td>Laboratory measurements</td>
</tr>
<tr>
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<td>López-Puertas et al. (1992)</td>
<td>Atmospheric retrieval</td>
</tr>
<tr>
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<td>Ratkowski et al. (1994)</td>
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<tr>
<td>$1.8 \times 10^{-12}$</td>
<td>Castle et al. (2006)</td>
<td>Laboratory measurements</td>
</tr>
<tr>
<td>$6.0 \times 10^{-12}$</td>
<td>Gusev et al. (2006)</td>
<td>Atmospheric retrieval</td>
</tr>
<tr>
<td>$1.5 \times 10^{-12}$</td>
<td>Huestis et al. (2008)</td>
<td>Recommended value</td>
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<td>$1.3-2.7 \times 10^{-12}$</td>
<td>Castle et al. (2012)</td>
<td>Laboratory measurements</td>
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Fig. 8 Sensitivity of 01101 and 02201 vibrational levels population to $k_{VT}$ for the five test daytime atmospheres: (a) SAW (twilight case), (b) MLW, (c) TROP, (d) MLS, e SAS. Solid black lines: kinetic temperature; red lines: calculations with $k_{VT} = 6.0 \times 10^{-12}$ cm$^3$ s$^{-1}$; blue lines: calculations with $k_{VT} = 1.5 \times 10^{-12}$ cm$^3$ s$^{-1}$; solid red and blue lines: populations of 01101 level, dashed red and blue lines: populations of 02201 level.
temperatures closer to the kinetic temperature profiles. The net heating rates for the five test atmospheres and their sensitivity to $k_{VT}$ are presented in Fig. 9a–d. As one can see, the absolute values of the net heating in the MLT are sensitive both to $k_{VT}$ and to the type of atmosphere. The latter is explained not only by temperature profile differences but also by variability of atomic oxygen VMR profiles. The $k_{VT}$ value and the atomic oxygen concentration are both equally important for the estimation of the MLT CO$_2$ radiative cooling and $I_{15\mu m}$ since the CO$_2$(v$_2$) quenching term contains their product (see Eq. (15) below). The strongest MLT cooling in Fig. 9 corresponds to high altitudes, high $k_{VT}$ rate, and polar latitudes in the summer hemisphere. The sensitivity to $k_{VT}$ grows with increasing altitude because the atomic oxygen concentration increases with height. Since the process (14) plays an important role in the MLT cooling, the best possible knowledge of $k_{VT}$ is required for adequate infrared cooling calculations. In the next section, we demonstrate an example of estimating $k_{VT}$ from atmospheric measurements and discuss the result with respect to the MLT energetics.

3.1.2 Estimating $k_{VT}$ Quenching Rate from Atmospheric Observations

The laboratory measurements of rate coefficients for various energy exchange processes by inelastic collisions of molecules and atoms suffer from difficulties with reproducing conditions close to those in the MLT in which molecules and atoms of various compounds interact. This is particularly true for laboratory studies of reactions involving oxygen atoms due to their extremely high chemical activity. On the other hand, the large variety of space and ground-based observations of the MLT available today provides an opportunity to utilize the MLT as “a natural laboratory” for retrieving these critical parameters. Below we discuss a recent example of the $k_{VT}$ retrieval which utilizes the synergy of coincidental satellite and lidar observations of the MLT. The advantage of utilizing the lidar (e.g., see Weitkamp 2005) for such experiments is that the lidar temperature retrievals $T(z)$ do not depend on the non-LTE model parameters and, therefore, can be used as references. The detailed description of the approach is given elsewhere (see Feofilov et al. 2012a).
comparison of the SABER temperature retrievals with lidar measurements has already
been performed by Remsberg et al. (2008), and the quenching rate coefficient used in that
study was estimated to be equal to \((6.0 \pm 3.0) \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}\). Applying stringent
overlapping criteria and treating the individual altitude layers of the overlapping region
separately, one can increase the accuracy and get into more detail of the MLT physics.

The general idea of the \(k_{VT}\) retrieval is in minimizing the difference between the
measured and simulated 15-\(\mu\)m radiation by varying the product of \(k_{VT}\) and \(O(3P)\) VMR.
For the study described, the measured radiation was provided by the SABER instrument
that also provides \(O(3P)(z)\) (see Smith et al. 2010) and \(CO_2(z)\) (see Rezac 2011) VMRs.
This dataset was supplemented with \(T(z)\) in 80–110 km altitude range measured by the Fort
Collins lidar (see She et al. 2003). For these temperature profiles, the 15-\(\mu\)m limb radiation
was simulated at each tangent height in the 85–105 km altitude interval, and the \(\chi^2\)
deviations (see Chap. 15 in Press et al. 2002) for the measured and simulated radiation
were built for the \(k_{VT}\) varying from \(1.0 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}\) to \(1.0 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}\) with a
\(5.0 \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}\) step. Figure 10 shows the averaged \(k_{VT}(z)\) “profile” obtained by
Feofilov et al. (2012a) that minimizes the radiation deviation.

Overall, the \(k_{VT}\) values shown in Fig. 10 fit the atmospheric retrievals well: the averaged
\(k_{VT} = (6.5 \pm 1.5) \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}\). However, Fig. 10 also shows the altitudinal
variability of \(k_{VT}\) that goes beyond its uncertainties in the 85–105 km altitude range.
Obviously, this variability does not imply that the rate coefficient depends on altitude.
Possible reasons for the \(k_{VT}\) “variability” are discussed in Feofilov et al. (2012a) and
include collisions with thermal and non-thermal hydrogen, electronically excited \(O(1S)\),
charged components, multi-quantum excitation of \(CO_2\) by thermal oxygen (Ogibalov
2000), and temperature dependence of the \(k_{VT}\). The authors suggest that the observed
phenomenon may be explained by the simplicity of the currently utilized \(CO_2\) non-LTE
model with respect to \(CO_2–O\) collisions. That might also be a clue to the “atmospheric/
laboratory” difference of the \(k_{VT}\) values. The standard pumping term in the non-LTE

![Figure 10: Solid line: \(k_{VT}(z)\) vertical distribution retrieved from minimizing the differences between the calculated and measured \(I_{15 \mu m}(z)\) radiation profiles (from Feofilov et al. 2012a). Dashed lines: uncertainties](image-url)
model, which describes the total production of CO₂ (v₂) in the state with the number of bending mode quanta v₂ due to collisions with the O(3P) atoms, has the form of

\[ Y_{v₂} = n_{O(3P)} \{ n_{v₂-1} k_{v₂-1,v₂} - n_{v₂} k_{v₂,v₂-1} \}, \tag{15} \]

where \( n_{O(3P)} \) is the O(3P) density, \( n_{v₂-1} \) and \( n_{v₂} \) are the vibrational states populations, and \( k_{v₂-1,v₂} \) and \( k_{v₂,v₂-1} \) are rate coefficients for one-quantum excitation and de-excitation, respectively.

In the current non-LTE models, including the one applied in this study, it is usually assumed that \( k_{v₂-1,v₂} = k_{0,1} \) and \( k_{v₂,v₂-1} = k_{1,0} = k_{VT} \). It follows from Huestis et al. (2008) that if the velocity distribution of O(3P) atoms is Maxwellian and their fine structure is thermalized, then the laboratory measured \( k_{0,1} \) and \( k_{1,0} \) are linked by the detailed balance relation:

\[ k_{0,1} = k_{1,0} \frac{g_1}{g_0} e^{-(E_1-E_0)/kT}, \tag{16} \]

where \( E_1 \) is the vibrational energy of the first \( v₂ \) vibrational level and \( E_0 \) is the energy of ground vibrational level. Sharma et al. (1994) showed that both aforementioned conditions are valid for O(3P) atoms in the Earth’s atmosphere up to at least 400 km, which seems to justify usage of (16) in the non-LTE models. However, as Balakrishnan et al. (1998) and Kharchenko et al. (2005) show, the non-thermal O(3P) and O(1D) atoms are produced by O₂ and O₃ photolysis and O₂⁺ dissociative recombination reactions in the MLT. These “hot” atoms may serve as an additional source of CO₂(v₂) level excitation. Therefore, the expression (15) may need to be replaced by an expression like

\[ Y_{v₂} = n_{O(3P)} \left\{ (1 - \alpha) \{ n_{v₂-1} k_{v₂-1,v₂} - n_{v₂} k_{v₂,v₂-1} \} + \alpha \left\{ \sum_y n_{v₂-y} k_{v₂,y,v₂-y}^{hot} - n_{v₂} \sum_y k_{v₂,y,v₂-y}^{hot} \right\} \right\}, \tag{17} \]

where \( \alpha \) is the altitude dependent fraction of total O(3P) density that corresponds to hot atoms and \( k_{v₂,y,v₂-y}^{hot} \) and \( k_{v₂,y,v₂-y}^{hot} \) are the rate coefficients for excitation and de-excitation of CO₂ molecules, respectively, due to collisions with hot atoms, assuming also multi-quantum processes. These rate coefficients are not related by the detailed balance since hot O(3P) atoms are not thermalized. Comparing (15), which is applied in the model used in the present study, with (17), one can see that the rate coefficient values retrieved in this work and also in earlier atmospheric studies are some sort of effective rate coefficients that include the contribution of hot O(3P) atoms, which may be expressed as

\[ k_{VT}^{ret}(z) = k_{VT}^{ret}(v₂-1,v₂) (1 - \alpha(z)) \cdot k_{v₂-1,v₂} + \alpha(z) \cdot \sum_y n_{v₂} k_{v₂,y,v₂}^{hot}. \tag{18} \]

These “hot” atoms may serve as an additional source of CO₂(v₂) level excitation that would explain the difference between the laboratory measurements and atmospheric retrievals of \( k_{VT} \). The increasing hot O(3P) atoms density with increasing altitude in the MLT may also explain the altitude dependence of the retrieved “efficient” \( k_{VT} \). We stress here that these important questions remain open and require further studies, both theoretical and experimental. The negative temperature dependence of \( k_{VT} \) that was found recently (see Castle et al. 2012) makes this problem more complicated since the altitude gradient of the \( k_{VT} \) parameter would be even higher if this “new” temperature dependence was to be used in the \( k_{VT} \) retrieval.
3.2 Ozone

The ozone molecule in its ground electronic state is a bent three-atomic molecule that has three vibrational modes: symmetric and asymmetric stretching modes (\(v_1\) and \(v_3\), respectively), and a bending mode (\(v_2\)). The \(v_1\) and \(v_3\) vibrations are close in energy (1,103 and 1,043 cm\(^{-1}\), respectively) and are coupled through a near-resonant V–V exchange. The radiative transitions corresponding to \(v_1\) and \(v_3\) quanta change are responsible for infrared cooling in the 9.6 \(\mu\)m O\(_3\) band. The \(v_2\) band transitions (705 cm\(^{-1}\)) are weak and overlap with 15 \(\mu\)m CO\(_2\) emissions. The transitions from the combination level (101) to the ground and hot transitions of the type \((v_1, v_2, v_3) \rightarrow (v_1 - 1, v_2, v_3 - 1)\) give rise to a strong 4.8-\(\mu\)m band. In modern non-LTE models of O\(_3\) (e.g., see López-Puertas and Taylor 2001; Kaufmann et al. 2006; Fernandez et al. 2009, 2010), the total number of vibrational levels considered is more than a hundred, up to the dissociation limit (~8,500 cm\(^{-1}\)), and includes many combination vibrational states. A simplified diagram of the first 22 vibrational levels of ozone and interactions between them is shown in Fig. 11. The non-LTE model for O\(_3\) molecule involves intra-molecular energy exchange processes:

\[
\begin{align*}
O_3(v_1, v_2, v_3) + M(N_2, O_2, O) &\xrightarrow{k_{\text{int}1}} O_3(v_1 - 1, v_2, v_3 + 1) + M \\
O_3(v_1, v_2, v_3) + M(N_2, O_2, O) &\xrightarrow{k_{\text{int}2}} O_3(v_1 - 1, v_2 + 1, v_3) + M \\
O_3(v_1, v_2, v_3) + M(N_2, O_2, O) &\xrightarrow{k_{\text{int}3}} O_3(v_1, v_2 + 1, v_3 - 1) + M
\end{align*}
\]

as well as V–T processes:

\[
\begin{align*}
O_3(v_1, v_2, v_3) + M(N_2, O_2, O) &\xrightarrow{k_{\text{VT}1}} O_3(v_1, v_2 - 1, v_3) + M \\
O_3(v_1, v_2, v_3) + M(N_2, O_2, O) &\xrightarrow{k_{\text{VT}2}} O_3(v_1 - 1, v_2, v_3) + M \\
O_3(v_1, v_2, v_3) + M(N_2, O_2, O) &\xrightarrow{k_{\text{VT}3}} O_3(v_1, v_2, v_3 - 1) + M
\end{align*}
\]

and intermolecular V–V processes:

\[
\begin{align*}
O_3(000) + N_2(v = 1) &\xrightarrow{k_{\text{VV}1}} O_3(000) + N_2(v = 0) + 130 \text{ cm}^{-1} \\
O_3(000) + O_2(v = 1) &\xrightarrow{k_{\text{VV}2}} O_3(100) + O_2(v = 0) + 456 \text{ cm}^{-1} \\
O_3(000) + O_2(v = 1) &\xrightarrow{k_{\text{VV}3}} O_3(001) + O_2(v = 0) + 517 \text{ cm}^{-1} \\
O_3(102) + O_2(v = 0) &\xrightarrow{k_{\text{VV}4}} O_3(000) + O_2(v = 2) - 4.9 \text{ cm}^{-1}.
\end{align*}
\]

A review of the rate coefficients for \(k_{\text{int}1} - k_{\text{int}3}\) (internal conversion of vibrational energy), \(k_{\text{VT}1} - k_{\text{VT}3}\) (V–T processes), and \(k_{\text{VV}1} - k_{\text{VV}4}\) (V–V processes) is given in Manuilova and Shved (1992), Manuilova et al. (1998), and López-Puertas and Taylor (2001). The relation between the rate coefficients is the following: \(k_{\text{int}1} \gg k_{\text{int}2} \approx k_{\text{int}3} \approx k_{\text{VT}1} \approx k_{\text{VT}2} \gg k_{\text{VT}3}\). Besides these processes and the radiative transitions shown in Fig. 11, the O\(_3\) vibrational levels are populated in the process of chemical recombination of ozone in the presence of a third body:

\[
O_2 + O(3P) + M \rightarrow O_3(v_1, v_2, v_3) + M,
\]

where \(M\) is N\(_2\), O\(_2\) or atomic oxygen. The energetics of this process is:
\[
\Delta H^0_f(O_2) + \Delta H^0_f(O^3P) = \Delta H^0_f(O_3) + E_{\text{vib}} + E_{\text{transl}}
\]

(30)

\[
E_{\text{vib}} + E_{\text{transl}} = 106.5 \text{ kJ/mol} = \sim 8,900 \text{ cm}^{-1},
\]

(31)

where \(\Delta H^0_f\) is the enthalpy of formation of gas at standard conditions, \(E_{\text{vib}}\) is the vibrational energy of \(O_3\), and \(E_{\text{transl}}\) is the total translational (kinetic) energy of \(O_3\) and \(M\). The values of \(\Delta H^0_f(O_2)\), \(\Delta H^0_f(O^3P)\), and \(\Delta H^0_f(O_3)\) used for estimating \(E_{\text{vib}} + E_{\text{transl}}\) in (30) were taken from the NIST Standard Reference Database (http://webbook.nist.gov/chemistry/).

As one can see from (31), the chemical energy released in the recombination process (29) can populate the \(O_3\) vibrational levels up to its dissociation limit. In reality, the fractioning between the \(E_{\text{vib}}\) and \(E_{\text{transl}}\) is complicated. Several models have been suggested for the nascent \(E_{\text{vib}}\) distributions. In a widely used “zero surprisal” model (e.g., see Levine and Bernstein 1974; Gil-Loéz et al. 2005), it is assumed that only \(O_3(0,0,v_3)\) levels are excited with the probability given by the formula:

\[
f(v) = \frac{(1 - E_v/D_e)^{1.5}}{\sum_{v=1}^{7} (1 - E_v/D_e)^{1.5}},
\]

(32)

where \(v\) and \(E_v\) are the level number and energy of \(v_3\), respectively, and \(D_e\) is the dissociation energy. In other models (see Kaufmann et al. 2006), it is considered that all the excitation goes to a single level \(v_3 = 3, 5,\) or 8. Fernandez et al. (2009, 2010) assume that the branching ratio between the \(E_{\text{vib}}\) and \(E_{\text{transl}}\) is 7:3 and that the vibrational excitation energy goes to \(v_3 = 6\). One can also assume that the chemical energy of the reaction (29) is used to excite the \(O_3(v_1, v_2, v_3)\) levels near the dissociation limit (the so-called “Top-8” model in López-Puertas and Taylor 2001).

The comparison of the effects of the nascent distribution model on the \(O_3(v_3)\) levels population is given in López-Puertas and Taylor (2001, Ch. 7.3.6, p. 211) where the vibrational temperatures for the first 7 \(v_3\) levels obtained with the zero surprisal model are
compared with that obtained with “Top-8” model where the excitation is distributed among the uppermost vibrational levels below the dissociation limit. The study shows the high sensitivity of the corresponding $v_3$ level populations to the model chosen. In the zero surprisal model, the atmospheric emission from the low $v_3$ levels is higher compared to that in the “Top-8” model and vice versa, the emissions from the high $v_3$ levels in the zero surprisal model are lower than that in the “Top 8” model. We have to stress here that if one assumes that the process (29) populates the O$_3$ levels close to the dissociation limit, then the rate coefficients for the processes (19)–(24) need to be determined since the rate coefficients $k_{\text{int}1} - k_{\text{int}3}$ and $k_{\text{VT}1} - k_{\text{VT}3}$ cannot be applied to high-energy levels due to anharmonicity of the vibrations and due to the complicated physics of closely spaced vibrational levels.

The uncertainty of the nascent population model is currently the most challenging problem for the interpretation of O$_3$ radiation measured in the hot bands (Manuilova, private communication, 2012). For example, if the O$_3$ VMR profile is retrieved from the radiation in the (010–000), (100–000) and (001–000) transitions that are less sensitive to the nascent populations model and then used for the interpretation of the 4.8-μm hot bands radiation measurements (see Kaufmann et al. 2006), an inconsistency arises: the calculated 4.8-μm radiation is 2–3 times lower than the measured one in the 50–75 km altitude interval. Correspondingly, Kaufmann et al. (2006) had to assume that either the ozone is formed at the levels around 3,000 cm$^{-1}$ (levels 003, 102, 201, or 300), like Manuilova et al. (1998) did, or that the $k_{\text{int}2}$, $k_{\text{int}3}$ rate coefficients for hot band transitions have to be reduced by a factor three or four to fit the MIPAS measurements. From the point of view of the infrared energy budget, the branching ratio between the $E_{\text{vib}}$ and $E_{\text{trans}}$ energies is noteworthy since the latter term directly adds to the atmospheric heating while the $E_{\text{vib}}$ is partially radiated back to the atmosphere and partially quenched and transformed to translational energy. This contribution to the heat reservoir may be found only by detailed solution of the non-LTE problem which accounts for the emission, propagation, absorption and re-distribution of radiative energy.

Figure 12 shows the vibrational temperatures of the (100) and (001) vibrational levels for the daytime and nighttime conditions calculated using the model of Manuilova et al. (1998). For most of the atmospheric scenarios, the breakdown of LTE for these levels starts at $\sim$65–70 km altitude. The vibrational temperatures shown in Fig. 12 are higher than the kinetic ones because of the recombination process (29) and the radiative pumping of the (100) and (001) levels by the absorption of radiation coming from the lower atmospheric layers and from the ground. The daytime increase of the vibrational temperatures shown in Fig. 12 is explained by a combined effect of higher daytime atomic oxygen VMR, higher O$_3$ VMR at 30–40 km, and lower O$_3$ VMR in the 50–75 km altitude interval.

The radiative pumping effects can be seen in Fig. 13 which shows that the net radiative effect of O$_3$ in the MLT area is heating that maximizes at $\sim$95 km altitude and varies from $\sim$0 K/day for the daytime cases to 3.0 K/day for the nighttime scenarios. Low absolute values of the net heating by O$_3$ in the MLT during daytime are explained by low O$_3$ VMRs (see solid lines in Fig. 6b). The energetic effects of ozone photolysis and subsequent energy transformation processes in the system of electronic-vibrational oxygen energy levels $O_2(b^3\Sigma_g^+, v)$, $O_2(a^1\Delta_e, v)$, and $O_2(X^3\Sigma^-, v)$ will be considered in the next section.

### 3.3 Molecular Oxygen and Ozone Photolysis

Absorption of solar ultraviolet radiation by O$_2$ and O$_3$ in the MLT leads to a whole chain of energy conversion processes. The first commonly accepted model of electronic kinetics of
O₂/O₃ photolysis products was developed by Harris and Adams (1983) and Thomas et al. (1984) and was significantly improved by Mlynczak et al. (1993). Later, this model was substantially extended by Yankovsky and Manuilova (2006). The updates and optimizations of this model may be found in Yankovsky and Babaev (2010) and Yankovsky et al. (2011). In this section, we will refer to the model of Yankovsky and Manuilova (2006) and demonstrate its coupling with the system of vibrational levels presented in Fig. 4.

The upper panel of Fig. 14 shows that the molecular oxygen photolysis caused by absorption of radiation in the Schumann-Runge continuum (175–205 nm) and Lyman-alpha (Ly-α) line leads to producing the electronically excited oxygen atoms O(1^D). These atoms are also produced as a result of O₃ photolysis in the Hartley band (200–310 nm). The collisions of O(1^D) with molecular oxygen in the ground electronic state, O₂ (X^3Σ^−, 0), and the transfer of its electronic energy to O₂ give rise to the populations of electronically vibrationally excited molecular oxygen O₂(b³Σ^+ , ν) with the subsequent redistribution of excitation energy to O₂(a¹Σ^+, ν) and O₂ (X^3Σ^−, ν) electronic-vibrational levels. These levels are also directly populated by O₃ photolysis in the Hartley band, Huggins bands (310–350 nm), and Chappuis bands (410–750 nm) and by resonance absorption of solar radiation at 762, 689, 629 nm and 1.27 μm. At each electronic-vibrational level, the deposited energy can be either quenched by a collision with one of the atmospheric species (mainly with N₂, O₂, and O) or radiated to the atmosphere. The net effect of solar absorption leading to O₂/O₃ photolysis is heating (h_{O₂/O₃}) since the energy is deposited in the respective region, and only part of it escapes through radiation in the 1.27 μm and 762 nm O₂ bands (see the cooling components in Fig. 15). The total energy budget of O₂/O₃ photolysis may be represented in the following form:

\[
h_{O₂/O₃}(z) = \frac{1}{C_p(z)\rho(z)} \left[ \int_{\lambda_{b1}}^{\lambda_{b2}} E_a(\lambda)\Phi_{sol}(\lambda, z)\sigma_a(\lambda)d\lambda + \int_{\lambda_{a1}}^{\lambda_{a2}} E_b(\lambda)\Phi_{sol}(\lambda, z)\sigma_b(\lambda)d\lambda - \sum_i h_v_i \Phi_i(z) \right],
\]

(33)
where $C_p(z)$ is the air heat capacity at constant pressure, $\rho(z)$ is the density, the indices $a$ and $b$ are related to $O_2$ and $O_3$ photodissociation, respectively, $E(\lambda)$ is the energetic effect of one photodissociation act calculated from the energy of the absorbed quantum and $\Delta H^0$ values of the participating atoms and molecules, and the amount of $\Phi_{\text{so}}(\lambda, z)$ is the incoming solar flux for wavelength $\lambda$ at the altitude $z$, $\sigma(\lambda)$ is the absorption cross section, $\Phi_i(z)$ and $h\nu_i$ are the integrated volume emission rates at the altitude $z$ and the energies of emission quanta that correspond to 630, 629, 689, 762, and 1.27 $\mu$m radiation (Fig. 14, upper panel).

Cross-sections for $O_2$ photodissociation have been the subject of numerous laboratory studies. Based on these studies, the parameterization schemes and tables for different spectral areas have been built: see Chabrillat and Kockarts (1997) for Ly-$\alpha$ radiation absorption; Minschwaner et al. (1992) and Kockarts (1994) for $O_2$ absorption in Schumann-Runge bands (175–205 nm); Nee and Lee (1997) and DeMajistre et al. (2001) for the absorption in Schumann-Runge continuum. Regarding the $O_3$ absorption cross-sections one can refer to: DeMore et al. (1997) for the absorption in Hartley band; Malicet et al. (1995) for Huggins bands; Brion et al. (1998) for Chappuis bands. The estimates of terms in (33) for the heating by the absorption of the UV solar radiation by $O_2$ and $O_3$ and for the 1.27 $\mu$m and 762 nm bands cooling (main cooling terms in (33)) are shown in Fig. 15. The cooling component is calculated from the 762 nm and 1.27 $\mu$m $\Phi_i(z)$ fluxes measured in the METEORS experiment (see Mlynczak et al. 2001). Heating rates due to $O_2$ and $O_3$ photodissociation for tropical conditions were estimated by Fomichev (2009) using the method suggested by Mlynczak and Solomon (1993) and Mlynczak and Marshall (1996). Overall, the net MLT heating due to photochemical effects of solar radiation on $O_2$ and $O_3$ is quite significant and can reach values of about 8 K/day at $\sim$ 95 km altitude. At the same altitude, both $O_2$ bands provide significant cooling of about 3.5 K/day.

The model of the $O_2/O_3$ photolysis product kinetics shown in the upper panel of Fig. 14 is implemented in the ALI-ARMS code (see Sect. 2.3). It allows simultaneous self-consistent solution of the non-LTE problem for the set of vibrational levels of molecules (Fig. 4) and the system of electronic-vibrational levels of the $O_2$ and $O_3$ molecules and electronic levels of O atoms. The coupling of the $O_2/O_3$ system of levels of Fig. 14 with

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{Fig_13.png}
\caption{Nighttime and daytime (twilight for the SAW case) net heating rates of ozone in the MLT region for the five test atmospheres: (a) SAW, (b) MLW, (c) TROP, (d) MLS, (e) SAS}
\end{figure}
Fig. 14 Joint scheme of O₂/O₃ photolysis products kinetics (upper panel, after Yankovsky and Manuilova (2006)) and H₂O vibrational levels (lower panel). In the upper panel thick horizontal lines correspond to electronic states of atomic and molecular oxygen; thin horizontal lines represent the vibrational substructure of the corresponding electronic state; lines with arrows in the upper part of the panel denote the O₂ and O₃ photolysis after absorption of radiation in the Schumann-Runge continuum (J SRC), Lyman-α line (J Ly α), Hartley (J H), Huggins (J H), and Chappuis (J Ch) bands (see text for more details). In the lower panel thick horizontal lines correspond to vibrational states of the H₂O molecule; optical transitions are shown as thin solid lines; dashed lines represent V–T processes, and thick dashed lines with arrows correspond to V–V energy exchange processes. Note the V–V coupling of the O₂ (X, v = 1) level in the upper panel and H₂O(010) level in the lower panel.
the molecular levels shown in Fig. 4 is realized through the V–V exchanges. In addition, the photochemical model is linked to the system of molecular levels shown in Figs. 2 and 4 through the O(1\textsuperscript{D}) energy transfer to N\textsubscript{2}(\textit{m}) vibrational levels, which are also pumped from the OH(\textit{m}) during nighttime. The V–V exchange between O\textsubscript{2}(1), N\textsubscript{2}(1) and H\textsubscript{2}O(010) shown in Fig. 14 dominates among these energy transfers and is important for the H\textsubscript{2}O model discussed in the next section.

3.4 Water Vapor

Water vapor cools the atmosphere in rotational and vibrational bands. The direct energetic effect of H\textsubscript{2}O on the MLT cooling is tertiary, compared to that of CO\textsubscript{2} and O\textsubscript{3}. However, besides the direct effects of infrared cooling, H\textsubscript{2}O influences the composition and energy budget of the MLT area in a number of ways. Being a source for chemically active constituents, such as OH, O(1\textsuperscript{D}), H\textsubscript{2}, and H (e.g., see Brasseur and Solomon 2005), it participates in the so-called “zero-cycle” reactions where the absorption of solar short-wave radiation leads to H\textsubscript{2}O photodissociation with subsequent recombination in a number of processes that result in heating of the atmosphere (e.g., see Sonnemann et al. 2005). The existence of water molecules at sufficiently low temperatures near the polar summer mesopause leads to the nucleation of ice particles in the MLT region (e.g., see Rapp and Thomas 2006, and references therein). These particles are responsible for such phenomena as noctilucent clouds (NLCs) and polar mesospheric summer echoes (PMSEs). Because of high sensitivity to local kinetic temperatures, the NLC and PMSE phenomena can be used as temperature probes for these regions (e.g., see Lübken et al. 2007; Petelina and Zasetsky 2009) and as possible indicators of climate change (e.g., see Thomas 2003).

In the gas phase, water molecule vibrations involve combinations of symmetric stretch (\textit{v}_1), covalent bond bending (\textit{v}_2), and asymmetric stretch (\textit{v}_3) modes with the band strength
ratio for the fundamental bands of the main H$_2$O isotope being 0.07/1.50/1.00 for the $v_1$, $v_2$, and $v_3$ vibrations, respectively (e.g., see Goody and Yung 1995, and references therein, and Rothman et al. 2009). The diagram in the lower panel of Fig. 14 shows the ground level and various excited vibrational levels of the H$_2$O molecule up to 7,445 cm$^{-1}$. The levels are marked in accordance with the number of vibrational quanta $v_1v_2v_3$. The rotational levels of H$_2$O are considered to be in LTE in the MLT while the vibrational levels start deviating from LTE above $\sim$ 50 km. The detailed description and sensitivity studies for the H$_2$O non-LTE model may be found in López-Puertas and Taylor (2001), Manuilova et al. (2001), and Feofilov et al. (2009). The highest sensitivity of the H$_2$O($v_2$) vibrational levels population is to the rate coefficient $k_{VV}$ of the V–V exchange process:

$$H_2O(v_2) + O_2(X^3\Sigma^-, 1) \xrightarrow{k_{VV}} H_2O(v_2 + 1) + O_2(X^3\Sigma^-, 0). \quad (34)$$

This sensitivity is bilateral: O$_2$(X$^3\Sigma^-$, 1) is pumped in a series of processes shown in the upper panel of Fig. 14; and reducing the value of the $k_{VV}$ coefficient may lead to a decrease in H$_2$O($v_2$) pumping. On the other hand, O$_2$(X$^3\Sigma^-$, 0) serves as a vibrational energy “reservoir” for H$_2$O($v_2$) quanta; reducing the $k_{VV}$ leads to decoupling of H$_2$O($v_2$) system from this reservoir and to an increase of H$_2$O($v_2$) populations. This issue is especially important when dealing with the interpretation of 6.6 $\mu$m H$_2$O radiation that will be described in Sect. 5.2.2. The $k_{VV}$ value estimated by different groups varies from $5.5 \times 10^{-13}$ cm$^3$ s$^{-1}$ (see Huestis 2006) through $1.0 \times 10^{-12}$ cm$^3$ s$^{-1}$ (see Koukouli et al. 2006) and $1.2 \times 10^{-12}$ cm$^3$ s$^{-1}$ (see Feofilov et al. 2009) to $1.7 \times 10^{-12}$ cm$^3$ s$^{-1}$ (see García-Comas et al. 2002); see also Table 2 in Feofilov et al. (2009) for a historical review of this rate coefficient.

Figure 16 shows the contributions of the main isotope H$_2$O rotational band (associated with the ground vibrational level) and vibrational bands to radiative heating of the MLT. As one can see, the net effect of the radiative transfer in the vibrational band in this region is heating since H$_2$O absorbs the radiation coming up from below where the net radiative effect is cooling (not shown in the figure due to the selected vertical axis limits). The vibrational band is responsible for a maximum of 0.5 K/day at $\sim$ 70 km altitude for the MLS and SAS profiles. On the other hand, the rotational band cools the mesosphere at 70–80 km and provides 0.6–1.5 K/day cooling in its maximum. It is interesting to note both quantitative and qualitative differences between the rotational cooling profiles for the SAW, MLW, TROP and MLS, SAS atmospheric scenarios. For the latter two, the cooling in the cold mesopause is compensated by absorption of the radiation coming from below. Summing up the profiles of the vibrational and rotational heating rates leads to reduction of the cooling effect of the rotational band in the 75–85 km altitude range to 1.5 K/day for the SAW, 1.1 K/day for the MLW and the TROP, 0.5 K/day for the MLS, and 0.2 K/day for the SAS atmospheric scenario. Above $\sim$ 85 km altitude, the H$_2$O contribution to the MLT energy budget becomes negligible for the SAW, MLW, TROP, and MLS scenarios due to the rapidly decreasing H$_2$O VMR. For the SAS atmosphere, the rotational band cooling at 100 km altitude remains on the order of 0.5 K/day due both to higher SAS temperatures here and higher summer H$_2$O VMR that is explained by the upward transport by vertical winds (see Garcia and Solomon 1994; Körner and Sonnemann 2001).

3.5 Radiative Cooling of the MLT Associated with Gravity Wave-Induced Atmospheric Fluctuations

An interesting aspect of the radiative cooling in the MLT is the combined effect of the small-scale fluctuations in the atmospheric vertical structure, and radiative transfer in the
15 μm CO₂ band. First described by Kutepov et al. (2007) for \( T(z) \) variations, it was later extended to the variation of \( T(z), \) CO₂(\( z \)), and O(\( ^3P \))(\( z \)) distributions (see Kutepov et al. 2012). The additional cooling in the MLT caused by this phenomenon is comparable with the heating effects of O₃ and H₂O, so we go into some detail regarding its mechanism. As one can see from the Sect. 3 of this work, the heating rates in the atmosphere strongly depend on the distributions of temperature and of radiatively active atmospheric components.

In the middle atmosphere, instantaneous profiles are highly irregular due to disturbances associated with gravity waves (GWs). The GW amplitude increases with height and the r.m.s. of temperature fluctuations is about 20 K at 90 km altitude (e.g., see Whiteway and Carswell 1995; Smith 2012). The wavelengths \( \lambda \ll 2\pi H \), where \( H \) is a scale height, are usually not well resolved in modern GCMs, and the dynamic effects of these “sub-grid” GWs are usually taken into account in the form of a “GW drag” parameterization (see Fritts and Alexander 2003). On the other hand, the atmospheric parameter fluctuations caused by GWs affect the radiative transfer and the corresponding heating rates. These effects, however, are usually omitted in GCMs because (a) small-scale GWs are not well resolved and (b) radiative heating rates \( h(z) \) parameterizations (see also Sect. 4) utilize a grid coarser than the grid of the GCM.

In the MLT, the trace gases CO₂ and O(\( ^3P \)) can be considered as conservative tracers so that the GW-induced variations are entirely due to adiabatic displacements of air parcels. In this case, one can express the trace gas VMR variation, \( \zeta' \), as a function of temperature variation \( T' \):

\[
\zeta' = \gamma T', \quad \gamma = \frac{d\zeta}{dz} \cdot \left( \frac{dT}{dz} + \frac{RT}{c_pH} \right)^{-1},
\]

where \( \zeta \) is the mean VMR, \( T \) is the mean temperature profile, and \( R \) is the gas constant. If the model for \( T' \) fluctuations is known, one can perform a numerical experiment to identify the effects of GW-induced fluctuations on mean radiative heating rate. This experiment was carried out for the five atmospheric scenarios. For each case, 1,000 individual GWs were generated in accordance with the statistical model described in Kutepov et al. (2007).
The ζ values were calculated in accordance with (35), and the non-LTE problem was run for each of the individual atmospheric profiles of T, O(^3P), and CO₂. After that, the differences of the heating rates Δh(z) = h(z) − h_{averm.}(z) were calculated where h(z) represents the h(z) averaged over 1,000 profiles and h_{averm.}(z) is the heating rate calculated for an averaged atmospheric profile. The r.m.s. profile of the temperature fluctuations

σ_T = \left[ \frac{1}{N} \sum_{i=1}^{N} (T_i')^2 \right]^{1/2}

for SAW atmospheric scenario is shown in Fig. 17a. The results presented in Fig. 17b show the combined effect of T, O(^3P) and CO₂ fluctuations on the CO₂ radiative heating. As one can see, the main effect of GW-induced fluctuations is an additional cooling of up to 3 K/day (for SAW and MLW) in the altitude region 80–95 km and a slight additional warming up to 1 K/day (for MLS). The observed effect is mainly related to temperature fluctuations and is explained by increased mean local thermal emission with respect to emission for the non-disturbed temperature due to strong non-linear temperature dependence of the Planck function (see Kutepov et al. 2007). Accounting for ζ_{CO₂} and ζ_{O(^3P)} fluctuations leads to changes in Δh(z) compared to the results obtained in Kutepov et al. (2007); ζ_{O(^3P)} fluctuation increases the additional cooling in the 85–100 km area by a maximum of ~1 K/day (SAW) while the ζ_{CO₂} fluctuation has the opposite effect, decreasing the h(z) in 88–100 km by ~1.7 K/day. These effects and their signs are related to ζ gradients in the MLT: according to (35), large ζ gradients lead to large ζ' values, and in the MLT the ζ_{O(^3P)} rapidly increases with height while the ζ_{CO₂} decreases with height (see Fig. 6a, d, respectively).

A more detailed explanation for the Δh(z) behavior with respect to temperature, ζ_{CO₂}, and ζ_{O(^3P)} fluctuations as well as its parameterization with respect to average temperature variation σ_T, and ζ_{CO₂}(z) and ζ_{O(^3P)}(z) distributions is given in Kutepov et al. (2012) who show that the net effect of these fluctuations can cause an additional cooling of up to 4 K/day near the mesopause.

4 Optimization of Heating Rate Calculation for GCMs

Let us assume that there are N_V vibrational levels involved in the problem and that the atmosphere is discretized at N_D altitude grid points. Solving the steady state equations (8) for this system requires solving the radiative transfer equation (4) for N_R spectral lines in the N_B ro-vibrational molecular bands. In the LBL approach for the non-overlapping lines, each line must be resolved in N_F frequency points to include the changes of the line shape with respect to atmospheric pressure and temperature. The above-mentioned parameters in modern models for molecules considered above are of the following order: N_V = 10–100, N_D ≈ 100, N_B = 10 – 1,000, N_R = 100 – 10^5, N_F = 10 – 100. Naturally, the exact non-LTE calculations performed in this manner cannot be used to estimate the heating rates h(z) in GCMs. Instead, the h(z) in molecular bands are usually calculated with the help of some parameterizations that take into account the main physical mechanism responsible for the radiative cooling or heating for each particular molecule. Obviously, there is a trade-off between accuracy and efficiency of these algorithms, most of which are described in the review paper of Fomichev (2009). Among these methods, one has to highlight the CO₂ infrared cooling parameterizations by Fomichev et al. (1993) and Fomichev et al. (1998a), which cover both LTE and non-LTE region starting from 15 km up to the altitudes in thermosphere. The non-LTE fraction of this algorithm (see Kutepov and Fomichev 1993).
evolved from the second-order escape probability approximation of Frisch and Frisch (1975) 
and was later supplemented by the parameterization of heating by the CO2 absorption of the 
near-infrared solar radiation (see Fomichev et al. 2004). The accuracy of this method in the 
MLT region is reported to be about 1 K/day if $k = 1.5 \times 10^{-12}$ cm$^3$ s$^{-1}$ is utilized (see 
Fomichev 2009). 

The 9.6 $\mu$m O3 cooling effects have not been parameterized yet due to the complexity of 
the O3 non-LTE model and its relatively small effect during the day. The same is also true 
for H2O. However, during the nighttime, the contribution of O3 to the MLT energy budget 
becomes noticeable (up to $\delta z$ K/day at $\sim 95$ km altitude, see Fig. 13), which calls for its 
parameterization in the GCM. The absence of this term might create a negative tempera-
ture bias at 85–100 km altitude.

Because of the increasing requirements for accuracy and flexibility of the radiative 
heating estimates in GCMs, it is unlikely that the parameterizations based on different 
approximate treatments of the non-LTE radiative transfer like various order escape 
probability approximations or matrix approaches (see Fomichev et al. 1993, 1998a) will 
satisfy the users. On the other hand, computer processor capacities as well as those of 
multi-core and parallel processing computers are continually increasing. This is supple-
mented also by the dramatic progress in the efficiency of exact multiple scattering non-
LTE radiative transfer algorithms (see Gusev and Kutepov 2003).

This allows turning from developing the radiative cooling parameterizations for GCMs 
to utilizing the exact non-LTE radiative transfer algorithms. Below, we describe an 
approach developed first for calculating $h(z)$ in the 15 $\mu$m CO2 bands in the Martian 
atmosphere (see Hartogh et al. 2005, Feofilov et al. 2006) and apply it to the terrestrial 
atmosphere. Since this scheme is based on our exact reference non-LTE model and the 
ALI-ARMS code, it is potentially applicable to any significant atmospheric molecule in the 
planetary atmosphere, given that the non-LTE reference model for this molecule exists.

Fig. 17 Additional cooling caused by atmospheric vertical structure fluctuations associated with gravity 
waves. (a) r.m.s. of the temperature variation caused by gravity waves for the SAW atmospheric scenario; 
(b) net effect of T(z), CO2(z), and O(z) variations on heating of the MLT region for the five test 
atmospheres: (a) SAW (twilight), (b) MLW, (c) TROP, (d) MLS, (e) SAS.
The acceleration approach consists of the three steps: (a) applying the ALI (for Accelerated Lambda Iteration) technique for radiative transfer; (b) replacing the radiative transfer in the \( N_R \) individual lines of the \( N_B \) molecular bands by radiative transfer in the molecular bands themselves by utilizing the opacity distribution function (ODF) method; and (c) reducing the \( N_V \) involved into the steady-state Eq. (8). The peculiarities of each step are discussed below.

4.1 Methods of Solving the Non-LTE Problem: The ALI Technique

The most straightforward way of solving the joint system of the SSE (8) and the RTE (4) is to iterate between them. This approach is traditionally called the “lambda iteration” (LI) and has been studied in detail in the astrophysical context since the 1920s (see Unsöld 1968). In atmospheric science, the straightforward application of this technique was described by Wintersteiner et al. (1992). This approach numerically simulates the multiple scattering of photons and is attractive since it involves \( N_D \) matrices of \( N_V \times N_V \) size. However, as Kutepov et al. (1998) showed, the convergence of the LI method is slow since the photons are “trapped” in the cores of optically thick lines. Kutepov et al. (1998) and Gusev and Kutepov (2003) studied the LI approach in detail for non-LTE problems in the Earth’s and planetary atmospheres and demonstrated that its convergence rate could be so slow that false solutions appear to be stable and/or the accumulation of numerical errors causes the process to diverge. They showed that the LI approach is particularly inefficient for the solution of the non-LTE problem in molecular bands, like those, for instance, for CO\(_2\) in the Earth’s and Martian atmospheres, since the general non-local and nonlinear nature of the non-LTE problem is aggravated here by the additional nonlinearity introduced by the V–V energy exchanges whose rates depend on the products of level populations.

An alternative way of solving the non-LTE problem is treating the SSE (8) and the RTE (4) simultaneously by discretizing the RTE with respect to an optical depth or pressure grid to get a matrix representation of the radiative terms in the SSE. In this approach (see, e.g., López-Puertas and Taylor 2001; Funke et al. 2012), the non-local radiative terms are expressed in terms of populations and the problem is solved iteratively as a set of non-local linear problems. The convergence of this method is usually fast (see Gusev and Kutepov 2003), but the time for filling out and inverting the matrices is large because of their size \((N_V \times N_D)\times (N_V \times N_D)\). From the point of view of computation time, one matrix iteration is roughly equivalent to \( N_D \) lambda iterations. However, if both \( N_D \) and \( N_V \) are large, each matrix iteration is very expensive in computer time; the same result may be achieved faster with LI or its accelerated version discussed below.

The problems related to the application of standard LI or matrix approaches outlined above are overcome by utilizing the so-called “accelerated lambda iteration” (ALI) method developed in stellar astrophysics (see Rybicki and Hummer 1991, 1992 and references therein). The family of ALI methods is based on the operator splitting of the form \( \Lambda = \Lambda^* + (\Lambda - \Lambda^*) \), where \( \Lambda \) is the monochromatic lambda operator \( \Lambda_{\mu \nu} \) along the ray with direction \( \mu \) defined by the formal solution of the RTE (4) \( I_{\mu \nu} = \Lambda_{\mu \nu}[S_{\nu}] \), where \( S_\nu = \eta_{\mu \nu}/\gamma_{\mu \nu} \) is the source function and the square brackets mean “acting on”. The splitting of the operator leads to the following iteration scheme: \( I_{\mu \nu}^{i+1} = \Lambda_{\mu \nu}^{i+1}[S_{\nu}] + (\Lambda_{\mu \nu}^{i+1} - \Lambda_{\mu \nu}^{i-1})[S_{\nu}^{i-1}] = \Lambda_{\mu \nu}^{i+1}[S_{\nu}] + I_{\mu \nu}^{\text{eff} \ i-1} \), where \( i \) and \( i-1 \) indices denote the current and the previous iterations, respectively, and \( I_{\mu \nu}^{\text{eff} \ i-1} = (\Lambda_{\mu \nu}^{i-1} - \Lambda_{\mu \nu}^{i-1})[S_{\nu}^{i-1}] \) is the “effective” intensity. Although this equation is only approximate at each iteration, it becomes exact for the converged solution, for which
\( S_v' = S_v^{i-1}, \Lambda_{\mu v}^{s i} = \Lambda_{\mu v}^{s i-1}, \) and \( \Lambda_{\mu v}^{i} = \Lambda_{\mu v}^{i-1} \). This iteration scheme describes a whole class of methods, each specified by the choice of a particular approximate lambda operator \( \Lambda_{\mu v}^{s i} \). The simplest choice is to use the diagonal part of the matrix representation of the exact lambda operator as it is done in the ALI-ARMS research code. Using a “preconditioning” approach (see Rybicki and Hummer 1991, 1992), one can rewrite the radiative rate coefficients in such a way that much of the transfer in the optically thick “core” of the line, described by the local part of the lambda operator, is canceled analytically:

\[
R_{\text{eff}}^{ll} = A_{ll}^{i} (1 - \Lambda_{ll}^{s i-1}) + B_{ll}^{i} \frac{J_{\text{eff}}^{ll}}{J_{\text{eff}}^{ll}},
\]

where \( \Lambda_{ll}^{s i} \) and \( J_{\text{eff}}^{ll} \) are obtained from \( \Lambda_{\mu v}^{s i} \) and \( I_{\text{eff}}^{ll} \) by applying double integration.

As a result, the ALI method converges much faster than the LI method while it still utilizes \( N_D \) matrices of \( N_V \times N_V \) size. The convergence speed of LI, matrix, and ALI methods has been studied in detail by Kutepov et al. (1998) who showed the superiority of ALI over the two other approaches for the atmospheres of Earth and Mars.

4.2 Optimizing the Radiative Transfer Calculations in Molecular Bands: Reducing the Number of Frequency Points

Additional significant computational time savings may be reached by optimizing the radiative transfer calculations. The latter linearly depends on the number of frequency and angle points in the angle and frequency integrals in (3). Whereas the number of angle points usually does not exceed 4, the number of frequency points is very large: the algorithm needs to treat the radiative transfer adequately in \( N_F \) points within each of \( N_R \) rotational-vibrational lines for each of \( N_B \) bands considered. If one considers the \( \eta(\nu) \) and \( \chi(\nu) \) (see Eq. (10)) for a group of lines belonging to one molecular band branch and builds them using the contributions of \( N_R \) individual lines \( \eta_{\nu}^{ll}(\nu) \) and \( \chi_{\nu}^{ll}(\nu) \), one will obtain the “spectral profile” characterized by non-monotonic behavior. In order to evaluate the integral of type (3), one has to consider this profile for a large number of frequency points. One of the ways of optimizing the radiative transfer for a molecular band would be to reduce the \( N_R \) by retaining strong lines and omitting weak lines. However, this will barely help and may lead to undesirable results for optically dense media since in this case the radiative transfer occurs mostly in the weak lines and partly in the far wings of strong lines.

In the LTE area, the reduction of frequency points number is usually achieved by utilizing the so-called CKD (correlated k-distribution) method that is based on grouping the gaseous spectral transmittances in accordance with the absorption coefficient \( k \). In this method, it is assumed that the \( k \)-distributions built for atmospheric layers with different pressure and temperature provide the spectral frequency correlation required for adequately reproducing the radiative transfer at any given frequency. In reality, the method appears to be accurate only in the case of radiative transfer between adjacent vertical levels or in the cases of low vertical temperature gradients. For flux calculations in the LTE area, it was found that the method is accurate to within 1 % (see Goody et al. 1989; Lacis and Oinas 1991; Fu and Liou 1992). However, the \( k \)-correlation scheme is not applicable in the case of non-LTE because the vibrational level populations involved in the building of \( k \)-distributions (and calculated in the LTE according to Boltzmann’s law for a local temperature) are unknown and depend on the solution of RTE.

In the context of non-LTE, one may use the idea of opacity distribution function (ODF), as discussed by Anderson (1987) and Mihalas (1978). In this approach, the absorption cross section is re-sampled to yield a monotonic function of frequency that can be represented by a relatively small number of frequency points. Though the idea is similar to the \( k \)-correlation, in this method, the absorption and emission profiles and the populations are...
treated separately, which allows accounting for the non-LTE conditions. There are two potential problems associated with this approach. First, the positions of the lines in the original and re-sampled \( \chi(v) \) distributions may be not the same since the re-ordering depends on the rotational distribution function in the ro-vibrational band, which, in turn, depends on temperature. The second problem is linked with the overlapping of two or more different molecular bands. Fortunately, these issues have little effect on the populations of the vibrational levels and radiative cooling and heating rates. The first problem is efficiently masked by photon trapping in the cores of thick lines and by relatively small changes in the temperature from layer to layer. The effects of the second problem can be neglected due to the validity of the non-overlapping lines approximation for the majority of applications in the MLT (see López-Puertas and Taylor 2001).

Since the use of the ODF approach for treating molecular bands is new, we provide some background information on it. If one considers a simple case of the non-overlapping branches of molecular bands, one can write the opacity and emissivity distributions for these spectral “profiles” as

\[
\eta_{v'v}(v) = \frac{h \nu_{v'v}}{4\pi} n_{v} A_{v'v}(T) \varphi_{v'v}(v),
\]

\[
\kappa_{v'v}(v) = \frac{h \nu_{v'v}}{4\pi} \left[ n_{v} B_{v'v}(T) \varphi_{v'v}^{a}(v) - n_{v} B_{v'v}(T) \varphi_{v'v}^{s}(v) \right],
\]

where \( A_{v'v}(T) \), \( B_{v'v}(T) \), and \( B_{v'v}(T) \) are the temperature-dependent Einstein coefficients for the branch, and \( \varphi_{v'v}^{e}(v) \), \( \varphi_{v'v}^{a}(v) \), and \( \varphi_{v'v}^{s}(v) \) are the normalized branch profile functions for emission, absorption, and stimulated emissions, respectively. We draw the reader’s attention to the fact that, compared to the CKD approach, the vibrational levels populations do not enter these branch profile functions. These profile functions are highly non-monotonic since they are constructed as superpositions of individual line profiles presented by the Voigt functions and weighted with the normalized rotational distribution.

Let us now define the \( \phi(v) \) functions as re-sampled and sorted \( \phi_{v'v}(v) \) profiles and also define normalized distributions

\[
\alpha(x) = \frac{1}{\phi(0)} \phi_{v'v} \left( \frac{1}{\phi(0)} x \right),
\]

where \( x = v \cdot \phi(0) \), and for which \( \alpha(0) = 1 \), \( \int_{0}^{+\infty} \alpha(x) \, dx = 1 \). We have built and analyzed several hundreds of these functions for linear molecules CO\(_2\), N\(_2\)O and CO fundamental and hot branches for broad ranges of pressure and temperature variations (\( P = 10^{-9} \) – 1 bar, \( T = 150–600 \) K).

Two principal conclusions, which followed from this analysis, are:

1) \( \varphi_{v'v}^{e}(v) \), \( \varphi_{v'v}^{a}(v) \), and \( \varphi_{v'v}^{s}(v) \) profiles for emission, absorption and stimulated emission of each branch nearly coincide (their relative differences do not exceed a few fractions of percent), and, therefore, may be represented by a single function \( \alpha(x) \), which we will call “ODF cross section” or simply “ODF”. Similar to the case of the complete frequency redistribution within a single line, when line absorption, emission, and stimulated emission in the line are described by the same Voigt function, this effect can be called “complete frequency redistribution” within the branch.

2) For the majority of the considered molecular bands of various molecules, the ODF cross-sections \( \alpha(x) \) for P, Q and R branches of perpendicular bands or those for P and
R branches of parallel bands are remarkably close. Although in the pressure and temperature ranges considered their relative differences in narrow intervals $\Delta x$ may reach 25 %, this has no significant effect on estimation of integrals of type (3). It allows operating with the single ODF cross section $\alpha(x)$ for each branch of any band of any of the linear molecules considered.

If the shape of the $\alpha(x)$ profile is known, then the Eqs. (36) and (37) may be rewritten for $\phi(v)$, which is a monotonic function that can be represented in a small number of frequency (or better to say “pseudo-frequency”) points $N_F$. This means that the ODF approach allows each branch to be replaced by a single “superline” of a special shape, which may be parameterized with respect to variations of pressure and temperature. Further analysis has shown that the “superline” can be approximated by a function similar to the Voigt function, in which $\exp(-y^2)$ is replaced by $\exp(-|y|)$.

The tests show that $N_F$ required for the sufficient accuracy of the RTE calculations when applying ODF is approximately equal to the number of frequency points for a single line in the LBL approach. Therefore, the utilization factor that can be reached by utilizing the ODF approach is roughly equal to the number of spectral lines within the branch ($\sim 100$ for CO$_2$, $\sim 1,000$ for O$_3$). The accuracy of the ODF approach with respect to heating rate calculations is shown in Fig. 18. As one can see, the errors for the net heating rate in CO$_2$ do not exceed $\pm 0.15$ K/day compared to the reference LBL data for all test atmospheres. This high accuracy of the radiative flux divergence calculations, which are extremely sensitive to the radiative transfer treatment, means that the ODF approach in its version outlined above significantly exceeds the CKD approach in its flexibility. Compared to CKD which provides reasonable accuracy only for adjacent atmospheric levels with low temperature gradient, the ODF approach demonstrates high accuracy over the wide altitude range of the MLT, where the temperature exhibits large changes with altitude.

We found that the higher accuracy of the ODF approach is explained by the much stronger dependence of the “superline” profile wing on temperature: the wing of the “superline” is proportional to $T^{-1}$ while the single Voigt line wing is proportional to $T^{-1/2}$. This temperature dependence efficiently compensates for the differences between the ODF and LBL approaches, associated with the radiative energy exchange between distant atmospheric layers having different temperatures.

4.3 Reducing the Number of Levels

For any of the methods described in Sect. 4.1, the time required for solving the problem depends on $N_V^2$; thus, reducing the number of vibrational levels involved in the non-LTE problem is desirable. On the other hand, the vibrational levels are involved in complicated chains of V–V, V–T, and radiative transfer processes, so any optimization should be performed with particular care. We have investigated the accuracy of day- and nighttime $h(z)$ calculations with respect to the number of vibrational levels involved. This study performed for five test atmospheres shows that for daytime non-LTE models of CO$_2$ the reduced set of vibrational levels that guarantees the 1 K/day accuracy (which is a typical requirement of modern GCMs) even for high values of CO$_2$–O quenching rate $k_{VT} = 6.0 \times 10^{-12}$ cm$^3$ s$^{-1}$ (see Sect. 3.1.2) includes 15 excited levels, some of which (so called “super-levels”) consist of vibrational levels closely spaced in energy and coupled by intensive intra-molecular V–V exchange. For these levels, we will use the notation $(v_1,2, m_3)$ where $v_{1,2} = 2v_1 + v_2$. In this notation, the levels for 626-th isotope are: $(1,0); (2,0); (3,0); (0,1); (4,0); (1,1); (2,1); (3,1); (4,1)$. For 636 and 628, the levels are $(1,0); (2,0); ...
(3,0). For the nighttime non-LTE model of CO₂, this set reduces to 11 excited levels and “super-levels”: (1,0); (2,0); (3,0); (0,1); (4,0); (1,1); (2,1) for 626 and (1,0) and (2,0) for 636 and 628. Figure 18 shows the accuracy of this approach for daytime calculations performed for five test atmospheres. In this plot, the non-LTE heating rates obtained in an optimized model are compared to that obtained for our “reference” model (5 isotopes, 60 vibrational levels). The blue lines in Fig. 18 show that the errors introduced by using an optimized model in 65–105 km interval do not exceed 0.3 K/day while the acceleration coefficient achieved is ~15 for daytime and ~25 for nighttime.

In summary, the total error associated with utilizing an optimized set of vibrational levels and applying the ODF technique for radiative transfer calculation in the molecular bands does not exceed ±0.35 K/day for any of the test atmospheres. The method is free from any constraints on the input profiles and can provide the $h(z)$ profiles for any altitude grid. The acceleration factor of $\sim 10^3$ compared to the “reference” LBL calculations allows its utilization in modern GCMs. The same approach may be used for optimizing the $h(z)$ calculations in O₃ and H₂O. The acceleration factor for ozone will be another order of magnitude higher because of the larger number of lines in the O₃ bands.

5 Infrared Sounding of the MLT Region

In Sect. 3, we primarily considered the energetic effects of the radiation emission and absorption on the atmosphere. The emission and absorption in molecular bands can also be used to estimate the atmospheric properties like temperature, pressure, concentration of optically active atmospheric components and even the concentration of optically passive components if these components affect the populations of the rotational and vibrational states of optically active molecules. The information about these characteristics is carried by the radiation that can be registered and processed to retrieve the desired atmospheric quantities. However, the MLT is a challenging region for measurements due to a number of...
reasons: (a) these heights cannot be reached by balloons or aircraft; (b) the total density and consequently the concentrations of atmospheric gases are low; (c) the vibrational, rotational, and spin levels populations start to depart from LTE thus reducing the “information content” of the radiation concerning these atmospheric layers; and (d) the temporal and spatial variability of the MLT region is high, which imposes certain criteria on the duration of the measurement. On the other hand, the high sensitivity of this region both to local and to non-local energy sources makes it a good indicator of atmospheric changes and attracts the attention of the researchers.

5.1 Atmospheric Observations in the MLT

The MLT observations can be separated into three groups: ground-based, in situ, and remote sensing from space. The measurements of the first two groups are confined to a local area while the satellite observations provide better coverage, up to global coverage. Direct ground-based sensing of the MLT region by measuring the atmospheric radiation coming to the ground is difficult because of the strong atmospheric absorption in the lower atmosphere. Lidars (for Light Detection and Ranging) overcome these difficulties by means of active sounding of the atmosphere at certain wavelengths and measuring the Rayleigh scattering, Raman scattering or fluorescence (e.g., see the overview book of Weitkamp (2005)). Using the time-resolved backscatter signal, one can retrieve the vertical distribution of the corresponding atmospheric property, such as kinetic temperature or the concentration of the trace gas. The typical accumulation time for the backscattered signal in modern lidars is on the order of tens of minutes, which is comparable to or is greater than the lifetime of the structures created by GW. Another limitation of the ground-based lidar techniques is the size of the area that can be observed (±100 km from the lidar setup). On the other hand, lidar techniques are robust, and the retrievals do not depend on sophisticated non-LTE models that makes the lidar measurements an excellent reference dataset in the MLT. Other reference data can be obtained from the in situ measurements performed by rockets (e.g., Goldberg et al. 2004 and references therein). The atmospheric observations of this type are also limited in space and time and cannot be used for building global distributions of pressure–temperature profiles or trace gas concentrations. In this respect, the satellite-based measurements look attractive since the absorption in the upper atmospheric layers is small compared to that in the lower atmosphere, and the coverage is global. As a result, in the past two decades, satellite instruments have become the dominant source of information regarding the Earth’s’ atmosphere in general and the MLT region in particular.

Figure 19 shows the three most common types of spaceborne observation techniques: detecting the atmospheric emissions in the limb scanning mode, registering the solar (or stellar) radiation attenuation by atmospheric absorption (the so-called occultation measurement mode), and measuring the atmospheric emissions and absorption of the terrestrial radiation in the nadir viewing mode. Compared to the other two techniques, the nadir mode is less suitable for the MLT observations. In this mode, the vertical distribution of the atmospheric properties is retrieved using the spectrally resolved radiation. The retrieval approach usually utilizes one of the modifications of Chahine’s method (e.g., see Chahine 1968, 1970, 1972; Smith 1970; Barcilon 1975; Houghton et al. 1984). In this approach, a thorough selection of a set of spectral channels is needed to reduce the background radiation effects and ensure proper contributions of the layers within the altitude measurement range.
In solar or stellar occultation measurements, the atmospheric parameters like density or trace gas VMRs are retrieved from the absorption profile. An obvious limitation of the occultation methods is the spatial and temporal coverage: typically the satellite instruments scan the atmosphere at sunset and sunrise once per orbit, with limited longitudinal coverage in each hemisphere. On the other hand, these methods are robust since the retrievals, in general, do not depend on the sophisticated non-LTE models: for a given molecular gas, the absorption is almost always defined by the transition from the ground state of the molecule, the concentration of which is much higher than that of other states of this molecule. The emission in the same band, which “reduces” the absorption, can be calculated in the LTE assumption for most of the cases. However, it was found that the non-LTE radiation contribution to the absorbed radiation measured by the SOFIE instrument (see Gordley et al. 2009) onboard the AIM platform (see Russell et al. 2009) is not negligible, and accounting for the non-LTE contribution in the 4.3 \( \mu \text{m} \) CO\(_2\) band is needed to extend the temperature retrievals up to \( \sim 110 \) km (see Marshall et al. 2011). Overall, the solar occultation instruments like HALOE (see Russell et al. 1993), ACE-FTS (see Bernath et al. 2005) and SOFIE have demonstrated a long-term record of reliable observations that can serve as an excellent reference dataset, with far better spatio-temporal coverage than may be obtained from local measurements.

The next step toward global measurements in the upper atmosphere is to study atmospheric emissions in the limb scanning mode. In this mode, collecting the atmospheric radiation along the long limb line of sight increases the signal-to-noise ratio; pointing to space instead of pointing to the ground in the nadir observation mode removes the intense background; the vertical resolution is defined by the optical properties of the observation setup and is about 2 km for modern instruments; the spatio-temporal coverage is limited only by the orbit of the satellite. Satellite limb measurements of atmospheric thermal emissions date back to the 1970s and instruments like the Limb Radiance Inversion Radiometer (LRIR) (see Gille et al. 1980), the Stratosphere and Mesosphere Sounder (SAMS) (see Drummond et al. 1980) and the Limb Infrared Monitor of the Stratosphere (LIMS) (see Gille and Russell 1984). Later on, the altitude range for this type of measurements was extended, and the infrared emissions affected by non-LTE were observed by the Cryogenic Limb Array Etalon Spectrometer (CLAES) (see Roche et al. 1993), the Improved Stratosphere and Mesosphere Sounder (ISAMS) (see Taylor et al. 1993), and the
Michelson Interferometer for Passive Atmospheric Sounding (MIPAS) (see Fischer et al. 2008), the CRISTA, and the SABER.

Figure 20 shows an example of atmospheric limb emissions measured by the SABER radiometers for daytime and nighttime conditions. The interpretation of these measurements requires the use of a corresponding non-LTE model and an inversion algorithm. Following the general formalism (see, e.g., Rodgers 2000), the relationship between the observed radiation profile $\tilde{I}$ and the state vector $\tilde{X}$, which is the concentration, temperature or the VMR of the atmospheric constituent, can be described as:

$$\tilde{I} = \tilde{F}(\tilde{X}) + \Delta\tilde{I},$$  \hspace{1cm} (39)

where $\tilde{F}(\tilde{X})$ is a nonlinear functional, which represents the forward radiance calculations in limb geometry and which includes known vertical distributions of atmospheric components and non-LTE model parameters, and $\Delta\tilde{I}$ is measurement error. We refer the reader to Rodgers (2000) for the review of inverse methods for atmospheric sounding. Here we consider the problem (39) in application to the MLT infrared measurements in limb geometry. The inversion of (39) in this case may be complicated due to the following reasons: (a) if the radiation at given tangent height depends on the radiation coming from other atmospheric layers, which is typical for the non-LTE conditions, the “information content” of the tangent point is reduced; (b) if the observed molecular band is optically thick, then the observed radiation remains constant or even decreases with decreasing tangent height, and the problem becomes ill-conditioned; (c) the response of limb radiation to a change in state vector (for example, an increase of temperature) can be positive (higher local temperature leads to higher population of the emitting levels) or negative (for hot bands, an increase in population of the lower level associated with higher temperature means an increase of the absorption).

Several research groups have developed retrieval algorithms for the infrared MLT observations: see, for example, Rinsland et al. (1992) for temperature, CO₂, and CO retrieval from ATMOS observations, López-Valverde et al. (1996) for CO retrieval from ISAMS measurements, Zaragoza et al. (2000) for the global distribution of CO₂ in the upper mesosphere from UARS/ISAMS observations, Mertens et al. (2001) and Gusev et al. (2006) for temperature retrievals from the SABER and CRISTA measurements, respectively, Kaufmann et al. (2002) for CO₂ and Grossmann et al. (2006) for CO retrieval from CRISTA measured spectra, Kaufmann et al. (2003) and Gil-López et al. (2005) for O₃ retrieval, Funke et al. (2009) for CO retrieval, Bermejo-Pantaleón et al. (2011) for temperature and NO, and García-Comas et al. (2011) for temperature retrievals in the MLT from MIPAS spectra, Mlynczak et al. (2007) for O₃ retrieval and Feofilov et al. (2009) for H₂O retrieval from the SABER, and Funke et al. (2005) for NO and NO₂ retrieval from the MIPAS measurements.

The majority of retrieval techniques applied for limb observations are based on the so-called “onion peeling” approach. This utilizes the specifics of limb geometry, namely that (neglecting aerosol scattering) atmospheric layers lying below the tangent height do not contribute to the measured signal. In this case, one only needs to solve a set of triangular matrices in order to get corrections to the chosen set of parameters. However, since in many cases, the tangent points are not observable (see case b) above), the rows of these matrices become linearly dependent, and the entire process collapses. In order to avoid this situation, various regularizations as well as a priori information are required to search for the so-called “physical solution”, which is one of pre-calculated solutions predicting the outgoing radiation within the accuracy of measurements. The search for such a solution is
usually organized as an iterative process. If the problem is nonlinear, then it is linearized, and the iterative search for the solution includes a latent iterative solution of the nonlinear problem, which often leads to time-consuming calculations and instabilities.

These complications stimulate the replacement of this inversion technique by more stable and reliable iterative forward-fit algorithm, in which the retrieval is performed iteratively. This approach avoids matrix inversion and relies on the stable and fast forward radiation calculations, a technique similar to the method described in Gordley and Russell (1981). Another advantage of the forward-fitting algorithm is that it allows straightforward accounting for the non-LTE conditions. The process starts with an initial guess for the $\tilde{X}$ profile assuming that the remaining atmospheric parameters are known and fixed. The non-LTE populations are calculated and used for the limb radiation calculations. The resulting simulated radiation vector $\tilde{I}_{\text{calc}}$ is compared to the measured radiation $\tilde{I}_{\text{meas}}$ at each tangent height, and $\tilde{X}$ is iterated using the following relaxation scheme:

$$
\tilde{X}^{i+1} = \tilde{X}^i + (\tilde{I}_{\text{meas}} - \tilde{I}_{\text{calc}}) \cdot W,
$$

where $i$ and $i+1$ denote two subsequent iterations and $W$ is a diagonal matrix, elements of which are inversely proportional to numerically calculated derivatives of the radiation produced by the forward model with respect to $\tilde{X}$ (see case c) above). After the $\tilde{X}^{i+1}$ vector is updated, it is used to calculate new non-LTE populations, and the radiation is simulated again. The iterations are repeated until the differences between the simulated and measured radiation become equal to the radiation noise for a given instrument. The computational cost of this method is higher than that of a standard inversion procedure. The approximate deceleration coefficient is roughly equal to the number of iterations (7–10 depending on the radiation noise and the molecule). However, the forward-fitting algorithms demonstrate

**Fig. 20** Example of the SABER/TIMED limb emissions for the tropical atmosphere (2008, day 198, $\text{lat} = 0 \pm 5^\circ$). Left panel nighttime measurements ($\theta_z > 120^\circ$ to exclude the effects of partial illumination of the upper atmosphere); right panel daytime measurements ($\theta_z < 85^\circ$ to exclude twilight conditions).
stable convergence and are less prone to false solutions (see Rezac et al. 2011 for recent findings on the convergence of relaxation type retrieval algorithms).

This method has been successfully applied by Gusev et al. (2006) to the non-LTE temperature retrievals in the Earth’s MLT from the CRISTA 15 μm spectral limb radiances, by Feofilov et al. (2009) to the H2O retrievals and Rezac (2011) to the CO2 retrievals from the SABER radiation measurements, as well as to the temperature retrievals in the Martian atmosphere from the MGS-TES observations (see Feofilov et al. 2012b).

5.2 Peculiarities of the Atmospheric Properties Retrievals from the Non-LTE Infrared Radiation Measurements

In this section, we demonstrate two examples of the non-LTE retrievals from the infrared radiation observations in the MLT. These retrievals are single-channel retrievals that are not complicated by the cross-correlation of the two or more channels (e.g., see Rezac 2011). Still, they show the complexity of the problem and the importance of the proper modeling of all the sinks and sources for the populations of the levels responsible for the radiation formation.

5.2.1 Importance of the ν2-Quanta V–V Exchange Between the CO2 Isotopes for Temperature Retrievals from 15 μm Radiation

For this example, we refer to Figs. 3, 7 and 8e of this work. It has been noticed that the retrieved SABER V1.06 temperatures for the polar summer mesospheric conditions (red curve in Fig. 5) differed significantly from those obtained from coincident falling sphere (FS) measurements taken during the 1–5 July 2002 summer MaCWAVE (for Mountain and Convective Waves Ascending VERTically) campaign (see Goldberg et al. 2004) and from the climatological profiles presented by Lübken (1999) for early July (compare the black, red, and green curves in Fig. 21b). Further evidence of a temperature discrepancy was obtained from the comparison of these temperatures with lidar data (e.g., see She et al. 2002; Fritts et al. 2004). One has to note that the polar summer temperature profile provides an excellent test bed for non-LTE codes due to a large difference between the mesopause and stratopause temperatures that may reach 150–180 K. Kutepov et al. (2006) have found that the discrepancy between the SABER V1.06 temperature retrievals and other measurements was caused by neglecting the V–V ν2-quanta exchange

\[
\text{CO}_2^i(01101) + \text{CO}_2^j(0) \leftrightarrow \text{CO}_2^i(0) + \text{CO}_2^j(01101)
\]

between the CO2(ν2) isotopic levels in the SABER V1.06 operational model, where i and j denote different isotopes. One has to note that the abundances of the CO2 isotopes in the Earth’s atmosphere are 0.98 for 626, 1.1 \times 10^{-2} for 636, 3.9 \times 10^{-3} for 628, 7.3 \times 10^{-4} for 627, and 4.4 \times 10^{-5} for 638 isotope. The low abundance of minor isotopes makes their spectral lines optically thin, which is crucial for the problem under consideration. In the summer polar atmosphere, the upwelling radiation from the warm stratosphere is absorbed by CO2 molecules of minor isotopes in and around the very cold mesopause, making \(T_{\text{vib}}\) of the 01101 minor isotopic levels there significantly warmer than the kinetic temperature. This is, however, not true for the 01101 level of main isotope 626: the fundamental 15 μm band of this isotope is optically thick—allowing the exchange of radiation only between the adjacent altitude levels and keeping this \(T_{\text{vib}}\) much closer to the kinetic temperature (see Sect. 2.2).
The radiative energy transferred to the mesopause in the optically thin isotopic bands populates the 01101 isotopic levels, which can radiate the 15 \( \mu \text{m} \) quanta, lose it in the collision with atomic oxygen or in the process of V–V energy transfer to the 01101 levels of the main isotope. The contributions of different isotopes to the 15 \( \mu \text{m} \) broadband limb radiation measured by the radiometer are shown in Fig. 21a. If the isotopic V–V exchange is not included in the model (it can be done for the convergence process acceleration, which is linked with the treatment of strongly coupled levels, see also Sect. 4.1), the isotopic 01101 levels become overpopulated and “produce” stronger 15 \( \mu \text{m} \) radiation in the model. Since the local temperature still has an effect on the populations of these levels (although weaker than in the LTE case), the retrieval algorithm decreases the local temperature to compensate for the increased radiation. The hydrostatic adjustment of pressure distribution in accordance with the new temperature profile moves the mesopause level downward. After the V–V exchange between CO2 isotopes was implemented into the SABER non-LTE operational model, significant reductions of the differences between the SABER retrievals and other measurements were observed (compare the blue and magenta curves with the green and red curves in Fig. 21b). This effect is noticeable at latitudes higher than 40° in both hemispheres in the summer period (June–August in the Northern hemisphere and December-February in the Southern hemisphere).

5.2.2 V–V Coupling of H2O(010) with O2(1) and the Effects of O2(1) Level Pumping

In Sect. 3.3, we considered a model of O2/O3 photolysis products and its coupling with the system of H2O vibrational levels (Fig. 14) through the V–V exchange process:

\[
\text{O}_2(X^3\Sigma^-, v = 1) + \text{H}_2\text{O}(v_2) \leftrightarrow \text{O}_2(X^3\Sigma^-, v = 0) + \text{H}_2\text{O}(v_2 + 1).
\]  

(42)

The importance of the V–V coupling of H2O(v2) with O2 (X3Σ−, v = 1) or, for simplicity, O2(1) level for correct estimating the H2O(010) level population and, therefore, for an adequate retrieval of the H2O VMR from the 6.3 \( \mu \text{m} \) radiation is well known (see Sect. 3.4).

Figure 22a shows the sensitivity of the H2O(010) population to the process (42) estimated for four test atmospheric scenarios (see Yankovsky et al. 2011). The most prominent
influence of processes (42) on the population of 010 is connected with the deactivation of vibrational levels 010, 020, 030, 110, 011, 040, 120 and 021 at near-resonance V–V energy exchange with O2(1) above 70 km, which leads to a significant decrease of the 010 level population at 80–85 km, in comparison with the population of the H2O(010) calculated without taking this process into account. Since the H2O and O2 systems are coupled, the next step is to include the pumping of O2(1) level through a set of processes shown in the upper panel of Fig. 14 and described in detail in Yankovsky and Manuilova (2006). However, including all these processes into the operational retrieval algorithm is too complicated and computationally expensive. Instead, the approximate quantum yield $\varepsilon$ for O2(1) molecules production per one act of O3 photolysis is used (e.g., see López-Puertas and Taylor 2001). In this approach, the value of quantum yield is equal to 4 and does not change with altitude. Recently, Yankovsky et al. (2011) used the model of Yankovsky and Manuilova (2006) and studied the behavior of the quantum yield $\varepsilon$ with respect to latitude, season, solar zenith angle, and O3 photolysis in the Hartley, Huggins, Chappuis and Wulf bands (200–900 nm). They found that $\varepsilon$ depends weakly on latitude, season, and solar zenith angle, and they suggested a simple parameterization formula for the altitude dependence of this parameter:

$$
\varepsilon = e^{a + b(\ln(P))^2 + cP},
$$

where $a = 2.1370 \pm 0.0328$, $b = -0.0366 \pm 0.00207$, and $c = -0.1099 \pm 0.0720$ are the parameterization coefficients, and $P$ is pressure in hPa.

The comparisons of variable $\varepsilon$ versus fixed $\varepsilon = 4$ calculations are shown in Fig. 22b. The behavior of the H2O(010) in this figure requires some comment. The 3–5 % increase in H2O(010) population at 60–70 km altitude is due to an increased pumping from O2(1) since $\varepsilon$ is greater than 4 here. However, the region above 80 km altitude also experiences an increase in H2O(010) population even though $\varepsilon$ is less than 4 at these heights. This is explained by the non-local nature of radiation in the MLT region: the H2O(010) levels in the mesopause are sensitive to radiation coming from other parts of the atmosphere. Increased quantum yield at 60–70 km altitudes leads to stronger pumping of the H2O(010) levels and, therefore, to an increase in 6.3 $\mu$m radiation coming up to the mesopause region. Correspondingly, this increased radiation leads to stronger excitation of the H2O(010) levels in the mesopause region. Neglecting the variability of $\varepsilon$ will lead to an overestimate of the retrieved H2O VMR in the MLT area by at least 5 %. The approach described has been incorporated into the H2O non-LTE model in the SABER operational code and will be used for H2O VMR retrievals in the next release of the SABER data.

6 Summary

This paper discusses the formation mechanisms of infrared radiation and its interaction with the matter in the mesosphere and lower thermosphere. A distinctive feature of this region is the breakdown of local thermodynamic equilibrium for the vibrational levels of the molecules involved in these mechanisms. Therefore, we concentrate mainly on the discussing the non-LTE models of IR radiation formation as well as on the methodology of the non-LTE problem solution with an aim to overview the current status of this methodology and corresponding applications for the energy budget calculations and interpretation of space observations, and indicate important, to our mind, directions of further activities.
The non-LTE models for three most important (for the MLT energy budget) molecules CO$_2$, O$_3$, and H$_2$O are described in detail, and the contributions of these molecules to the radiative energy budget are estimated for five test atmospheres, ranging from polar winter to polar summer. As it was shown in a number of studies, CO$_2$ is the main cooler of the MLT: the cooling increases with increasing altitude up to about 110–130 km (depending on the atmospheric model) reaching maxima of the order of tens of K/day. The LTE breakdown for CO$_2$(v$_2$) levels occurs at altitudes above $\sim$ 85 km and the magnitude of the cooling strongly depends on the CO$_2$(v$_2$)–O quenching rate coefficient. However, there is an unresolved discrepancy between the laboratory measurements and atmospheric retrievals of this rate coefficient. We address this problem and describe recent attempt to estimate this coefficient from atmospheric measurements, which obviously indicates the need for further theoretical and experimental studies of this collisional process.

For O$_3$, the net effect is cooling at altitudes below $\sim$ 70 km and heating above $\sim$ 75 km, which reaches 2–3 K/day at $\sim$ 90–95 km altitude. The combined effect of the rotational and vibrational H$_2$O bands in the MLT region is a cooling of $\sim$ 1.0–1.5 K/day at $\sim$ 75 km; this cooling decreases with increasing altitude. We also address a new term of the energy budget, namely, the additional radiative cooling caused by fluctuations of the atmospheric vertical structure induced by small-scale (sub-grid) gravity waves, which are poorly resolved in the current GCMs and show that it can reach $\sim$ 4 K/day at the mesopause altitude.

Another problem addressed in this paper is the efficiency and accuracy of the IR radiative heating rate estimations. The radiative heating rates in modern GCMs are usually parameterized. A number of efficient parameterization schemes have been developed up to now, which, however, have limited accuracy and flexibility. In this paper, we propose a way for optimizing exact algorithms of the non-LTE heating rate calculations for further usage in GCMs aimed at keeping the accuracy and flexibility of LBL calculations. Three key steps of this optimization are (a) utilizing accelerated lambda iterations (ALI) as the most advanced technique for solving the non-LTE problem, (b) using the opacity distribution function (ODF) approach for treating the branches of molecular bands as single

![Fig. 22](image_url) Tests (Yankovsky et al. 2011) showing the importance of correctly accounting for the V–V exchanges with O$_2$(X, v = 1) in the H$_2$O non-LTE model: (a) sensitivity of H$_2$O(010) level population to H$_2$O(010)–O$_2$(X, v = 1) coupling for four test atmospheric scenarios; (b) sensitivity of H$_2$O(010) level population to the efficiency of O$_2$(X, v = 1) level pumping from the O$_2$/O$_3$ photolysis products (Sect. 3.3); the H$_2$O(010) populations computed with variable quantum yield $\varepsilon$ are compared with the H$_2$O(010) populations estimated with $\varepsilon = 4$ (see text)
spectral “super-lines”, and (c) reducing the number of vibrational levels. As we show, these three features ensure an efficient and flexible calculation algorithm with controlled accuracy that can be used in modern GCMs as a replacement for parameterizations.

Another important aspect addressed in the paper is the quality of non-LTE models applied for the interpretation of the infrared emissions observations of the MLT region. These models require precise and detailed accounting for all known mechanism of molecular vibration excitation, exchange and quenching. To illustrate that, we use the SABER infrared limb observations in the 15 µm and 6.3 µm channels and the corresponding $T(z)$ and $H_2O(z)$ retrievals. We show that omission of the process of $V-V v_2$ quanta exchange between the main and “minor” CO$_2$ isotopes (~1.5 % in abundance in total) leads to a ~10 K underestimate of the mesopause temperature for polar summer conditions. We also demonstrate how simplification of the O$_2$(1) level pumping in the O$_2$/O$_3$ photolysis products kinetics scheme leads to an underestimate of the 6.3 µm H$_2$O radiation between 50 and 70 km altitude and, correspondingly, to 5–10 % overestimate of H$_2$O VMR retrieved from 6.3 µm radiation measured in this region.

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